

Bilateral Operating Gain Circles

Gonzalez Example 3.7.1

Parameters for Example 3.7.1

$$j := \sqrt{-1} \quad dB := 1 \quad G_P := 9 \cdot dB$$

$$M := \begin{bmatrix} 0.641 & 0.057 \\ 2.058 & 0.572 \end{bmatrix} \quad \phi := \begin{bmatrix} -171.3 \cdot \text{deg} & 16.3 \cdot \text{deg} \\ 28.5 \cdot \text{deg} & -95.7 \cdot \text{deg} \end{bmatrix} \quad m := 1..2 \quad n := 1..2 \quad S_{m,n} := M_{m,n} \cdot e^{j \cdot (\phi_{m,n})}$$

$$\Delta := S_{1,1} \cdot S_{2,2} - S_{2,1} \cdot S_{1,2} \quad |\Delta| = 3.014 \cdot 10^{-1} \quad \arg(\Delta) = 1.099 \cdot 10^2 \cdot \text{deg}$$

$$K := \left[\frac{1 - (|S_{1,1}|)^2 - (|S_{2,2}|)^2 + (|\Delta|)^2}{2 \cdot |S_{1,2} \cdot S_{2,1}|} \right] \quad K = 1.504 \quad g_P := \frac{10^{(1 \cdot G_P)}}{(|S_{2,1}|)^2} \quad g_P = 1.875$$

$$r_P := \frac{\sqrt{1 - 2 \cdot K \cdot |S_{1,2} \cdot S_{2,1}| \cdot g_P + (|S_{1,2} \cdot S_{2,1}|)^2 \cdot g_P^2}}{|1 + g_P \cdot [(|S_{2,2}|)^2 - (|\Delta|)^2]|} \quad r_P = 4.309 \cdot 10^{-1}$$

$$C_P := \frac{g_P \cdot S_{2,2} - \Delta \cdot \overline{(S_{1,1})}}{1 + g_P \cdot [(|S_{2,2}|)^2 - (|\Delta|)^2]} \quad |C_P| = 5.083 \cdot 10^{-1} \quad \arg(C_P) = 1.039 \cdot 10^2 \cdot \text{deg}$$

$$\theta := -32 \cdot \text{deg} \quad \Gamma_L := C_P + r_P \cdot e^{j \cdot \theta} \quad |\Gamma_L| = 3.595 \cdot 10^{-1} \quad \arg(\Gamma_L) = 4.748 \cdot 10^1 \cdot \text{deg}$$

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$$\Gamma_{in} := S_{1,1} + \frac{S_{2,1} \cdot S_{1,2} \cdot \Gamma_L}{1 - S_{2,2} \cdot \Gamma_L} \quad \left| \Gamma_{in} \right| = 6.29 \cdot 10^{-1} \quad \arg(\Gamma_{in}) = -1.755 \cdot 10^2 \cdot \text{deg} \quad \Gamma_S := \overline{\Gamma_{in}}$$

$$\text{Mag}_{\Gamma_a} := \left| \frac{\Gamma_{in} - \overline{\Gamma_S}}{1 - \Gamma_{in} \cdot \Gamma_S} \right| \quad \text{Mag}_{\Gamma_a} = 0 \quad \text{VSWR}_{in} := \frac{1 + \text{Mag}_{\Gamma_a}}{1 - \text{Mag}_{\Gamma_a}} \quad \text{VSWR}_{in} = 1$$

$$\Gamma_{out} := S_{2,2} + \frac{S_{2,1} \cdot S_{1,2} \cdot \Gamma_S}{1 - S_{1,1} \cdot \Gamma_S} \quad \left| \Gamma_{out} \right| = 6.697 \cdot 10^{-1} \quad \arg(\Gamma_{out}) = -1.027 \cdot 10^2 \cdot \text{deg}$$

$$\text{Mag}_{\Gamma_b} := \left| \frac{\Gamma_{out} - \overline{\Gamma_L}}{1 - \Gamma_{out} \cdot \Gamma_L} \right| \quad \text{Mag}_{\Gamma_b} = 6.219 \cdot 10^{-1} \quad \text{VSWR}_{out} := \frac{1 + \text{Mag}_{\Gamma_b}}{1 - \text{Mag}_{\Gamma_b}} \quad \text{VSWR}_{out} = 4.289$$

$$G_P := \left[\frac{1}{\left| 1 - \left(\Gamma_{in} \right)^2 \right|} \right] \cdot \left(\left| S_{2,1} \right| \right)^2 \cdot \left[\frac{1 - \left(\left| \Gamma_L \right| \right)^2}{\left(\left| 1 - S_{2,2} \cdot \Gamma_L \right| \right)^2} \right] \quad G_P = 7.943 \quad G_{P_{dB}} := 10 \cdot \log(G_P) \quad G_{P_{dB}} = 9 \cdot \text{dB}$$

$$G_T := \left[\frac{1 - \left(\left| \Gamma_S \right| \right)^2}{\left(\left| 1 - \Gamma_{in} \cdot \Gamma_S \right| \right)^2} \right] \cdot \left(\left| S_{2,1} \right| \right)^2 \cdot \left[\frac{1 - \left(\left| \Gamma_L \right| \right)^2}{\left(\left| 1 - S_{2,2} \cdot \Gamma_L \right| \right)^2} \right] \quad G_T = 7.943 \quad G_{T_{dB}} := 10 \cdot \log(G_T) \quad G_{T_{dB}} = 9 \cdot \text{dB}$$