

Bilateral Operating Gain Circles

Gonzalez Example 3.7.2

Parameters for Example 3.7.2

$$j := \sqrt{-1} \quad dB := 1 \quad G_P := 10 \cdot dB$$

$$M := \begin{bmatrix} 0.500 & 0.080 \\ 2.500 & 0.800 \end{bmatrix} \quad \phi := \begin{bmatrix} -180 \cdot \text{deg} & 30 \cdot \text{deg} \\ 70 \cdot \text{deg} & -100 \cdot \text{deg} \end{bmatrix} \quad m := 1..2 \quad n := 1..2 \quad S_{m,n} := M_{m,n} \cdot e^{j \cdot (\phi_{m,n})}$$

$$\Delta := S_{1,1} \cdot S_{2,2} - S_{2,1} \cdot S_{1,2} \quad |\Delta| = 2.228 \cdot 10^{-1} \quad \arg(\Delta) = 6.212 \cdot 10^1 \cdot \text{deg}$$

$$K := \left[\frac{1 - (|S_{1,1}|)^2 - (|S_{2,2}|)^2 + (|\Delta|)^2}{2 \cdot |S_{1,2} \cdot S_{2,1}|} \right] \quad K = 3.991 \cdot 10^{-1} \quad g_P := \frac{10^{(1 \cdot G_P)}}{(|S_{2,1}|)^2} \quad g_P = 1.6$$

$$r_L := \left| \frac{S_{1,2} \cdot S_{2,1}}{(|S_{2,2}|)^2 - (|\Delta|)^2} \right| \quad r_L = 3.388 \cdot 10^{-1} \quad C_L := \frac{\overline{(S_{2,2} - \Delta \cdot \overline{S_{1,1}})}}{[(|S_{2,2}|)^2 - (|\Delta|)^2]} \quad |C_L| = 1.177 \quad \arg(C_L) = 9.718 \cdot 10^1 \cdot \text{deg}$$

$$r_P := \frac{\sqrt{1 - 2 \cdot K \cdot |S_{1,2} \cdot S_{2,1}| \cdot g_P + (|S_{1,2} \cdot S_{2,1}|)^2 \cdot g_P^2}}{|1 + g_P \cdot [(|S_{2,2}|)^2 - (|\Delta|)^2]|} \quad r_P = 4.733 \cdot 10^{-1}$$

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$$C_p := \frac{\overline{g_p \cdot S_{2,2} - \Delta \cdot (\overline{S_{1,1}})}}{1 + g_p \cdot [(\overline{S_{2,2}})^2 - (|\Delta|)^2]} \quad |C_p| = 5.717 \cdot 10^{-1} \quad \arg(C_p) = 9.718 \cdot 10^1 \cdot \text{deg}$$

$$\theta := -82.8 \cdot \text{deg} \quad \Gamma_L := C_p + r_p \cdot e^{j\theta} \quad |\Gamma_L| = 9.843 \cdot 10^{-2} \quad \arg(\Gamma_L) = 9.708 \cdot 10^1 \cdot \text{deg}$$

$$\Gamma_{in} := S_{1,1} + \frac{S_{2,1} \cdot S_{1,2} \cdot \Gamma_L}{1 - S_{2,2} \cdot \Gamma_L} \quad |\Gamma_{in}| = 5.205 \cdot 10^{-1} \quad \arg(\Gamma_{in}) = -1.793 \cdot 10^2 \cdot \text{deg} \quad \Gamma_s := \overline{\Gamma_{in}}$$

$$\text{Mag}_{\Gamma_a} := \left| \frac{\Gamma_{in} - \overline{\Gamma_s}}{1 - \Gamma_{in} \cdot \Gamma_s} \right| \quad \text{Mag}_{\Gamma_a} = 0 \quad \text{VSWR}_{in} := \frac{1 + \text{Mag}_{\Gamma_a}}{1 - \text{Mag}_{\Gamma_a}} \quad \text{VSWR}_{in} = 1$$

$$\Gamma_{out} := S_{2,2} + \frac{S_{2,1} \cdot S_{1,2} \cdot \Gamma_s}{1 - S_{1,1} \cdot \Gamma_s} \quad |\Gamma_{out}| = 9.341 \cdot 10^{-1} \quad \arg(\Gamma_{out}) = -9.718 \cdot 10^1 \cdot \text{deg}$$

$$\text{Mag}_{\Gamma_b} := \left| \frac{\Gamma_{out} - \overline{\Gamma_L}}{1 - \Gamma_{out} \cdot \Gamma_L} \right| \quad \text{Mag}_{\Gamma_b} = 9.203 \cdot 10^{-1} \quad \text{VSWR}_{out} := \frac{1 + \text{Mag}_{\Gamma_b}}{1 - \text{Mag}_{\Gamma_b}} \quad \text{VSWR}_{out} = 2.41 \cdot 10^1$$

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$$G_P := \left[\frac{1}{\left| 1 - \Gamma_{in} \right|^2} \right] \cdot \left| S_{2,1} \right|^2 \cdot \left[\frac{1 - \left| \Gamma_L \right|^2}{\left| 1 - S_{2,2} \cdot \Gamma_L \right|^2} \right]$$

$$G_P = 10$$

$$G_{P_dB} := 10 \cdot \log(G_P) \quad G_{P_dB} = 10 \cdot \text{dB}$$

$$G_T := \left[\frac{1 - \left| \Gamma_s \right|^2}{\left| 1 - \Gamma_{in} \cdot \Gamma_s \right|^2} \right] \cdot \left| S_{2,1} \right|^2 \cdot \left[\frac{1 - \left| \Gamma_L \right|^2}{\left| 1 - S_{2,2} \cdot \Gamma_L \right|^2} \right]$$

$$G_T = 1 \cdot 10^1$$

$$G_{T_dB} := 10 \cdot \log(G_T) \quad G_{T_dB} = 1 \cdot 10^1 \cdot \text{dB}$$