

SOLUTIONS MANUAL

MICROWAVE TRANSISTOR AMPLIFIERS

Analysis and Design

SECOND EDITION

Guillermo Gonzalez



PRENTICE HALL

Upper Saddle River, NJ 07458

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Simon & Schuster / A Viacom Company
Upper Saddle River, New Jersey 07458

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Printed in the United States of America

10 9 8 7 6 5 4 3 2 1

ISBN 0-13-271255-5

Prentice-Hall International (UK) Limited, *London*
Prentice-Hall of Australia Pty. Limited, *Sydney*
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Editora Prentice-Hall do Brasil, Ltda., *Rio de Janeiro*

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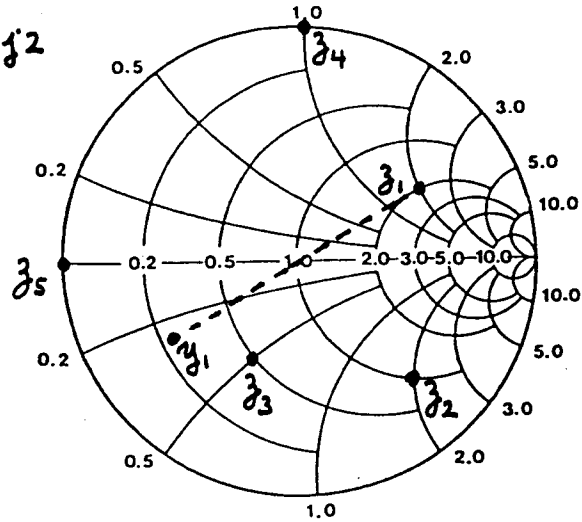
2.1) (a) LET $z_1 = \frac{Z}{50} = \frac{100 + j100}{50} = 2 + j2$

(z_1 IS SHOWN IN THE SMITH CHART)

(b) $y_1 = \frac{1}{z_1} = 0.25 - j0.25$

(y_1 IS SHOWN IN THE SMITH CHART)

(c) IN THE ZY SMITH CHART THE LOCATION OF z_1 IS THE SAME AS IN (a). THE VALUE OF y_1 IS READ FROM THE GREEN CIRCLES.



(d) $z_2 = \frac{50 - j100}{50} = 1 - j2$

$y_2 = \frac{1}{z_2} = 0.2 + j0.4$

$z_3 = \frac{25 - j25}{50} = 0.5 - j0.5$

$y_3 = \frac{1}{z_3} = 1 + j$

$z_4 = j\frac{50}{50} = j1$

$y_4 = \frac{1}{z_4} = -j1$

$z_5 = j0$

$y_5 = \infty$

(z_2, z_3, z_4 , AND z_5 ARE SHOWN IN THE SMITH CHART)

2.2) (a) $z = -r + jx$, $\Gamma = \frac{z-1}{z+1} = \frac{-(r+1) + jx}{(1-r) + jx}$ (1)

$|\Gamma| = \frac{\sqrt{(r+1)^2 + x^2}}{\sqrt{(1-r)^2 + x^2}} = \left[\frac{r^2 + 2r + 1 + x^2}{r^2 - 2r + 1 + x^2} \right]^{1/2}$ (2)

IN (1) THE NUMERATOR IS GREATER THAN THE DENOMINATOR, SINCE $2r > -2r$. HENCE, $|\Gamma| > 1$

(b) FROM (1): $\frac{1}{\Gamma^*} = \frac{(1-r) - jx}{-(r+1) - jx} = \frac{(r-1) + jx}{(r+1) + jx}$ (3)

EQ. (3) IS IDENTICAL TO THE TRANSFORMATION IN (2.2.2) WHERE $z = r + jx$ WITH $r \geq 0$. HENCE, NEGATIVE RESISTANCES CAN BE HANDLED IN THE SMITH CHART BY PLOTTING $\frac{1}{\Gamma^*}$ AND INTERPRETING THE RESISTANCE CIRCLES AS BEING NEGATIVE, AND THE REACTANCE CIRCLES AS MARKED.

$$(c) \quad Z_1 = \frac{Z_1}{Z_0} = \frac{-20 + j16}{50} = -0.4 + j0.32$$

FROM THE SMITH CHART WE READ:

$$\frac{1}{\Gamma^*} = 0.47 \angle 139^\circ$$

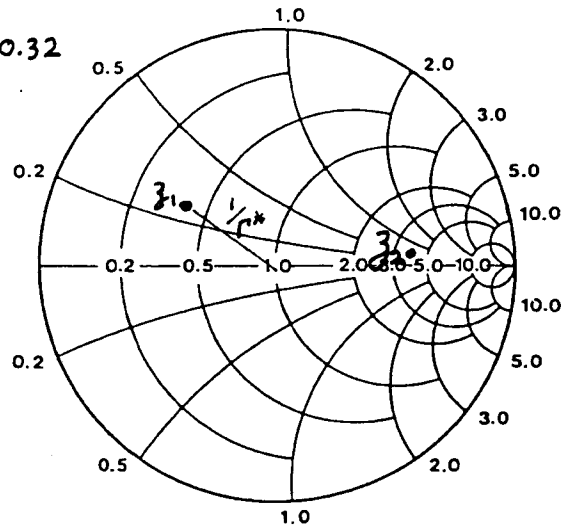
$$\text{HENCE } \Gamma = 2.1 \angle 139^\circ$$

FOR:

$$Z_2 = \frac{-200 + j25}{50} = -4 + j0.5$$

$$\frac{1}{\Gamma^*} = 0.61 \angle 3.75^\circ$$

$$\text{HENCE } \Gamma = 1.6 \angle 3.75^\circ$$



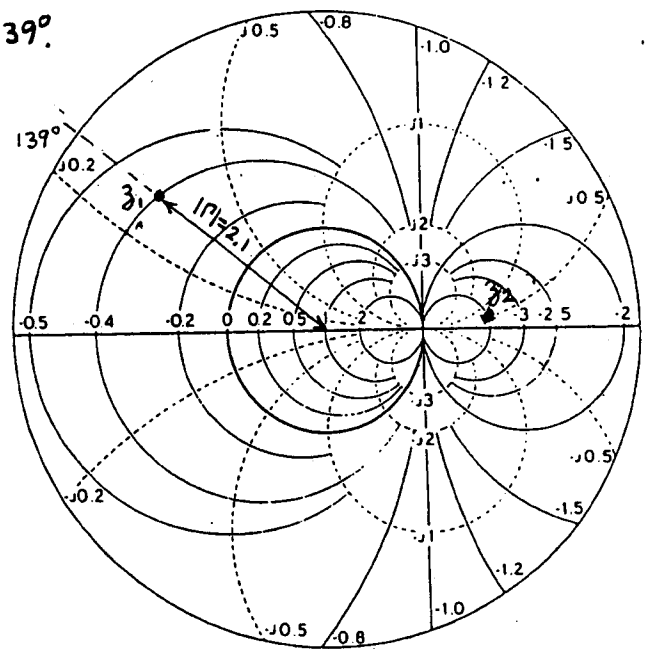
(d) SEE THE COMPRESSED SMITH

CHART. FOR $Z_1 = -0.4 + j0.32$

WE READ: $|\Gamma| = 2.1$, $\angle \Gamma = 139^\circ$.

HENCE $\Gamma = 2.1 \angle 139^\circ$.

SIMILARLY, FOR Z_2 WE OBTAIN $\Gamma = 1.6 \angle 3.75^\circ$



$$(e) \quad |\Gamma| \approx 3.2$$

$$2.3) \quad Z(d) = Z_0 \frac{Z_L + j Z_0 \tan \beta d}{Z_0 + j Z_L \tan \beta d}$$

$$Z(d + \frac{\eta \lambda}{2}) = Z_0 \frac{Z_L + j Z_0 \tan(\beta d + \frac{\eta \beta \lambda}{2})}{Z_0 + j Z_L \tan(\beta d + \frac{\eta \beta \lambda}{2})}$$

$$; \eta \beta \frac{\lambda}{2} = \frac{\eta 2\pi \lambda}{\lambda \frac{\lambda}{2}} = \eta \pi$$

$$\tan(\beta d + \eta \pi) = \tan \beta d$$

Hence,

$$Z(d + \frac{\eta \lambda}{2}) = Z(d)$$

2.4) FROM (2.2.6) AND (2.2.7): LET $\Gamma_0 = |\Gamma_0| e^{j\phi_0}$, THEN
 $\Gamma = \Gamma_0 e^{-j2\beta d} = |\Gamma_0| e^{j(\phi_0 - 2\beta d)} = |\Gamma| e^{j\phi}$; $|\Gamma| = |\Gamma_0|$
 $\phi = \phi_0 - 2\beta d$
 $Z(d) = Z_0 \left[\frac{1 + |\Gamma| e^{j\phi}}{1 - |\Gamma| e^{j\phi}} \right]$

$$= Z_0 \left[\frac{1 + |\Gamma| \cos \phi + j |\Gamma| \sin \phi}{1 - |\Gamma| \cos \phi - j |\Gamma| \sin \phi} \right] \quad (1)$$

$$= Z_0 \left[\frac{1 - |\Gamma|^2 \cos^2 \phi - |\Gamma|^2 \sin^2 \phi + j 2 |\Gamma| \sin \phi}{(1 - |\Gamma| \cos \phi)^2 + (|\Gamma| \sin \phi)^2} \right]$$

OR

$$Z(d) = Z_0 \left[\frac{1 - |\Gamma|^2 + j 2 |\Gamma| \sin \phi}{1 - 2 |\Gamma| \cos \phi + |\Gamma|^2} \right] = R(d) + j X(d)$$

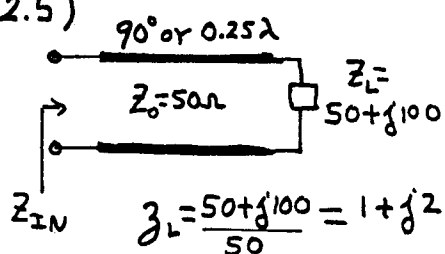
$$\text{HENCE: } R(d) = Z_0 \frac{1 - |\Gamma|^2}{1 - 2 |\Gamma| \cos \phi + |\Gamma|^2}, \quad X(d) = Z_0 \frac{2 |\Gamma| \sin \phi}{1 - 2 |\Gamma| \cos \phi + |\Gamma|^2}$$

ALSO, FROM (1)

$$|Z(d)| = Z_0 \left[\frac{(1 + |\Gamma| \cos \phi)^2 + (|\Gamma| \sin \phi)^2}{(1 - |\Gamma| \cos \phi)^2 + (|\Gamma| \sin \phi)^2} \right]^{1/2} = Z_0 \left[\frac{1 + 2 |\Gamma| \cos \phi + |\Gamma|^2}{1 - 2 |\Gamma| \cos \phi + |\Gamma|^2} \right]^{1/2}$$

$$\theta_d = \tan^{-1} \frac{X(d)}{R(d)} = \tan^{-1} \left[\frac{2 |\Gamma| \sin \phi}{1 - |\Gamma|^2} \right]$$

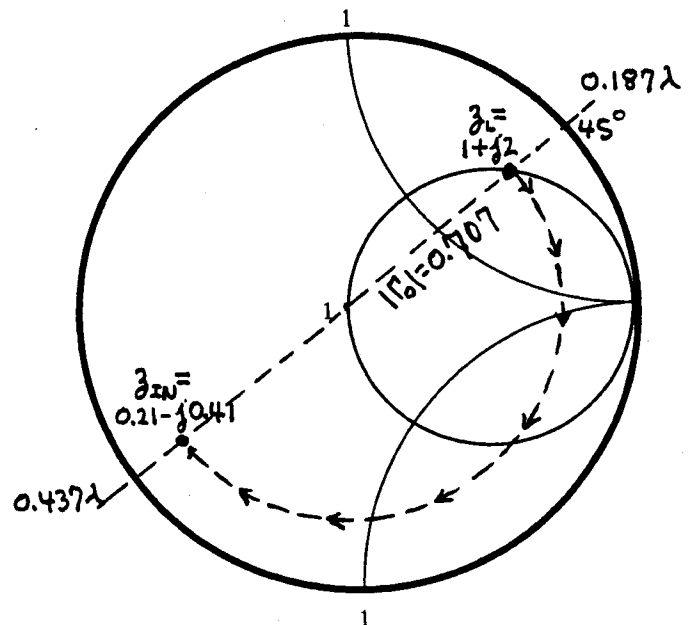
2.5)



LOCATE Z_L IN THE SMITH CHART.
 AT Z_L READ 0.187λ . DRAW A
 CONSTANT $|\Gamma|$ CIRCLE. Z_{IN} IS
 AT 0.25λ FROM Z_L (OR
 $0.187\lambda + 0.25\lambda = 0.437\lambda$).
 HENCE: $Z_{IN} = 0.21 - j0.41$
 $Z_{IN} = 50 Z_{IN} = 10.5 - j20.5 \Omega$

$$\Gamma_0 = 0.707 \angle 45^\circ$$

$$VSWR = \frac{1 + 0.707}{1 - 0.707} = 5.83$$



$$2.6) (a) |V(d)|_{\max} = |A| (1 + |\Gamma_0|) \text{ AND } |I(d)|_{\min} = \frac{|A|}{Z_0} (1 - |\Gamma_0|)$$

$$\text{HENCE: } R(d)_{\max} = \frac{|V(d)|_{\max}}{|I(d)|_{\min}} = Z_0 \frac{1 + |\Gamma_0|}{1 - |\Gamma_0|}$$

$$r(d)_{\max} = \frac{R(d)_{\max}}{Z_0} = \frac{1 + |\Gamma_0|}{1 - |\Gamma_0|} = \text{VSWR}$$

$$(b) |V(d)|_{\min} = |A| (1 - |\Gamma_0|) \text{ AND } |I(d)|_{\max} = \frac{|A|}{Z_0} (1 + |\Gamma_0|)$$

$$\text{HENCE: } R(d)_{\min} = \frac{|V(d)|_{\min}}{|I(d)|_{\max}} = Z_0 \frac{1 - |\Gamma_0|}{1 + |\Gamma_0|}$$

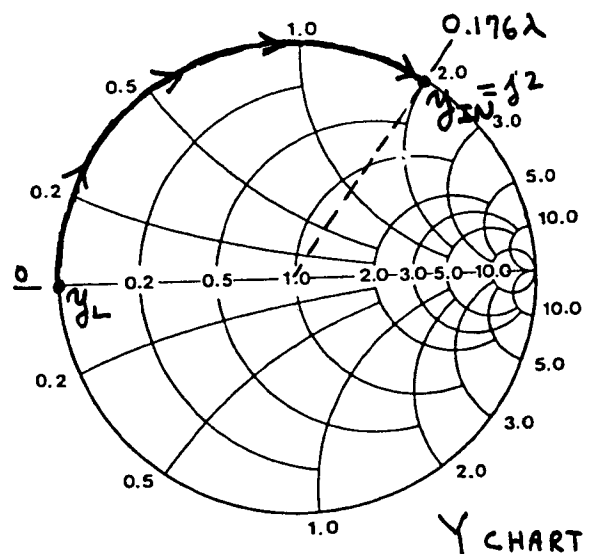
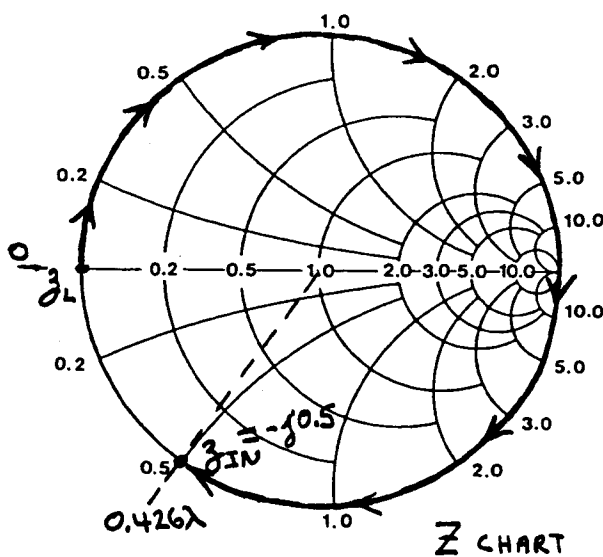
$$r(d)_{\min} = \frac{R(d)_{\min}}{Z_0} = \frac{1 - |\Gamma_0|}{1 + |\Gamma_0|} = \frac{1}{\text{VSWR}}$$

$$2.7) (a) z_{IN} = -j \frac{25}{50} = -j0.5$$

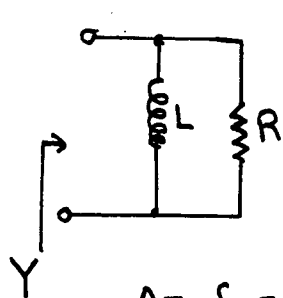
$$\text{FROM THE } Z \text{ SMITH CHART: } l = 0.426\lambda$$

$$(b) y_{IN} = j2$$

$$\text{FROM THE } Y \text{ SMITH CHART: } l = 0.176\lambda$$



2.8) THE FREQUENCY RESPONSE FOLLOWS A CONSTANT CONDUCTANCE CIRCLE WITH $g=1$. THE EQUIVALENT CIRCUIT IS (SEE FIG. 2.3.2b)



$$Y = \frac{1}{R} - \frac{j}{\omega L}$$

$$y = \frac{Y}{Y_0} = Y Z_0 = \frac{Z_0}{R} - j \frac{Z_0}{\omega L}$$

$$g = 1 = \frac{Z_0}{R} \Rightarrow R = 50 \Omega$$

$$\text{AT } f_b = 1 \text{ GHz: } -j \frac{50}{\omega_b L} = -j 0.5, L = \frac{50}{0.5(2\pi 10^9)} = 15.9 \text{ nH}$$

$$\text{OBSERVE THAT AT } f_a = 500 \text{ MHz: } y = -j \frac{Z_0}{\omega_a L} = \frac{-j 50}{2\pi 500 \times 10^6 \times 15.9 \times 10^{-9}} = j 1$$

2.9) (a) $Y = 0.4$, $R = 50r = 50(0.4) = 20 \Omega$

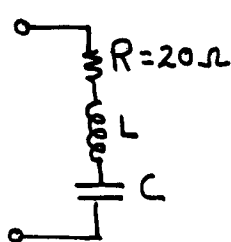
AT f_a , THE REACTANCE IS $-j 0.6$; AND AT f_b IS $-j 0.32$.

$$Z = 20 - \frac{j}{\omega C} \quad \therefore \frac{1}{\omega_a C} = 0.6(50) = 30 \quad (C = 50 \text{ pF})$$

$$\text{OR } f_a = \frac{1}{2\pi(30) 50 \times 10^{-12}} = 106.1 \text{ MHz}$$

$$\text{AND } \frac{1}{\omega_b C} = 0.32(50) = 16 \Rightarrow f_b = \frac{1}{2\pi(16) 50 \times 10^{-12}} = 198.9 \text{ MHz}$$

(b) THE EQUIVALENT CIRCUIT IS A SERIES R, L, C CIRCUIT.



$$\text{AT } f_a = 500 \text{ MHz, } Z = 20 + j 10$$

$$\therefore 20 + j 10 = R + j \left(\omega_a L - \frac{1}{\omega_a C} \right) \quad (1)$$

$$\text{AT } f_b = 1 \text{ GHz, } Z = 20 + j 30$$

$$\therefore 20 + j 30 = R + j \left(\omega_b L - \frac{1}{\omega_b C} \right) \quad (2)$$

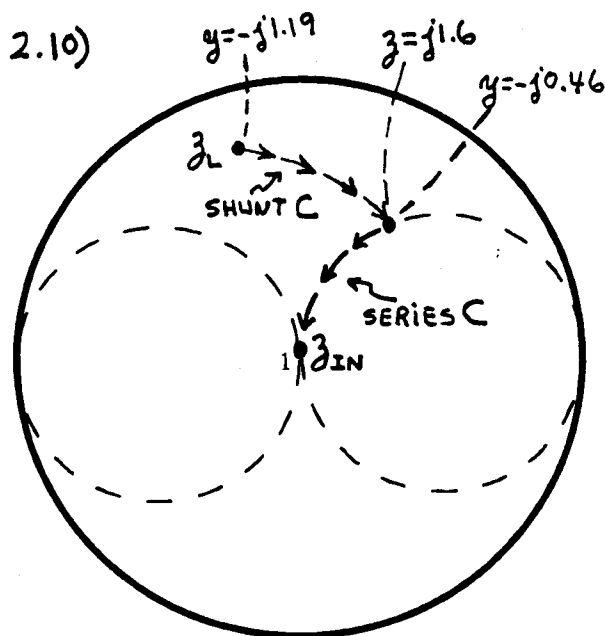
FROM (1) AND (2) IT FOLLOWS THAT $R = 20 \Omega$ AND

$$10 = 2\pi \left(f_a L - \frac{1}{f_a C} \right) \text{ AND } 30 = 2\pi \left(f_b L - \frac{1}{f_b C} \right)$$

THE SIMULTANEOUS SOLUTION OF THESE EQUATIONS IS:

$$L = 5.31 \text{ nH}$$

$$C = 47.64 \text{ pF}$$

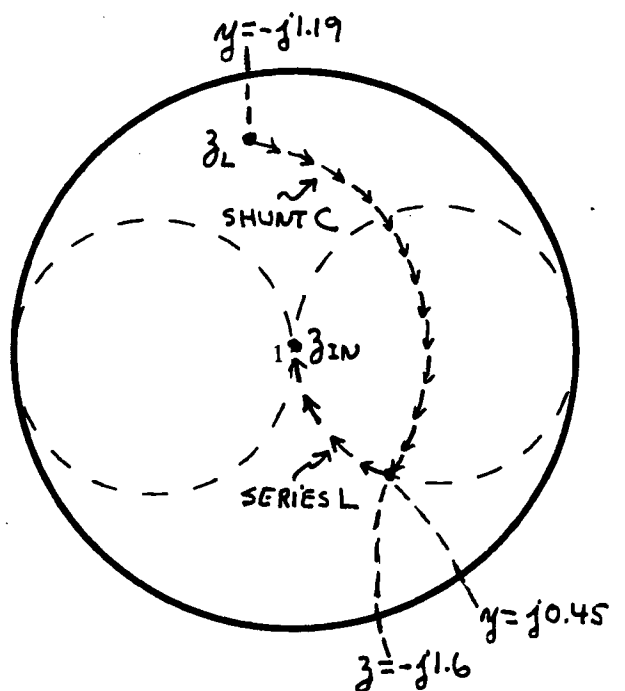
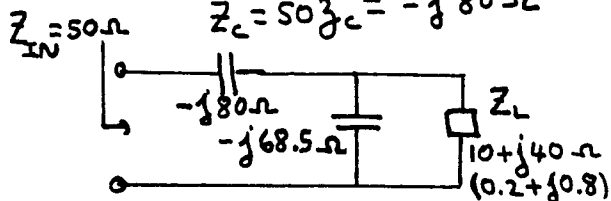


SHUNT C: $y_c = -j0.46 - (-j1.19) = j0.73$

$Z_c = \frac{50}{y_c} = -j68.5 \Omega$

SERIES C: $z_c = 0 - j1.6 = -j1.6$

$Z_c = 50 z_c = -j80 \Omega$

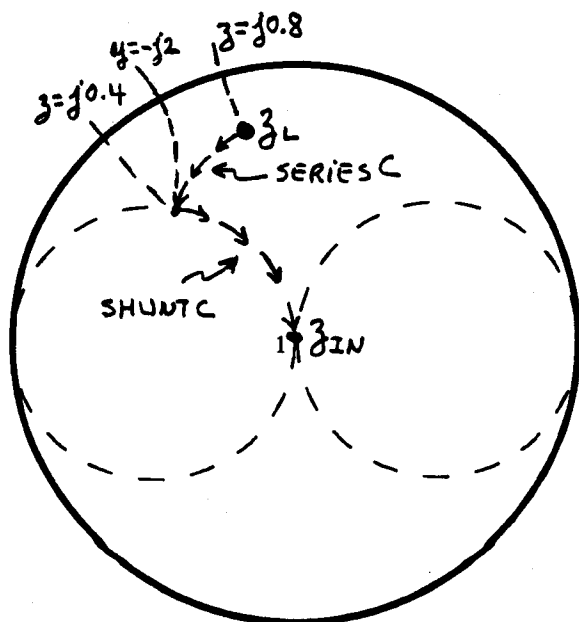
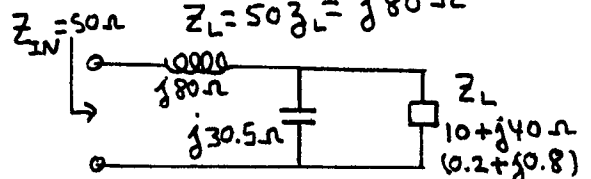


SHUNT C: $y_c = j0.45 - (-j1.19) = j1.64$

$Z_c = \frac{50}{y_c} = -j30.5 \Omega$

SERIES L: $z_c = 0 - (-j1.6) = j1.6$

$Z_c = 50 z_c = j80 \Omega$

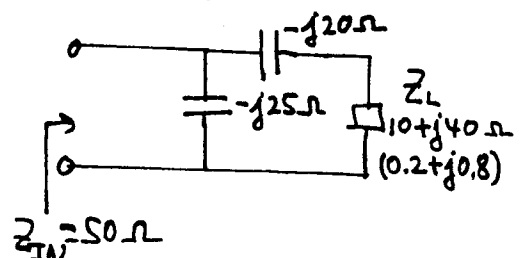


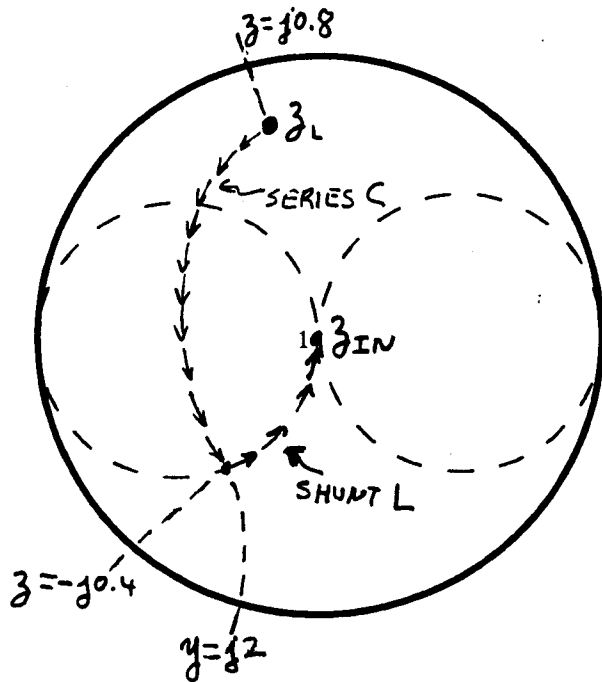
SERIES C: $z_c = j0.4 - j0.8 = -j0.4$

$Z_c = 50 z_c = -j20 \Omega$

SHUNT C: $y_c = 0 - (-j2) = j2$

$Z_c = \frac{50}{y_c} = -j25 \Omega$



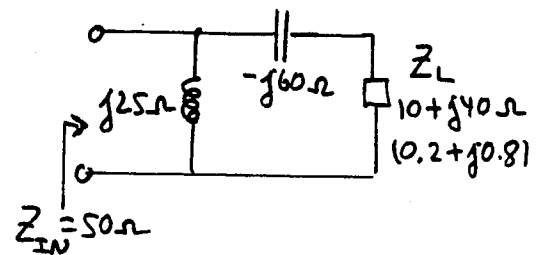


$$\text{SERIES C: } Z_C = -j0.4 - j0.8 = -j1.2$$

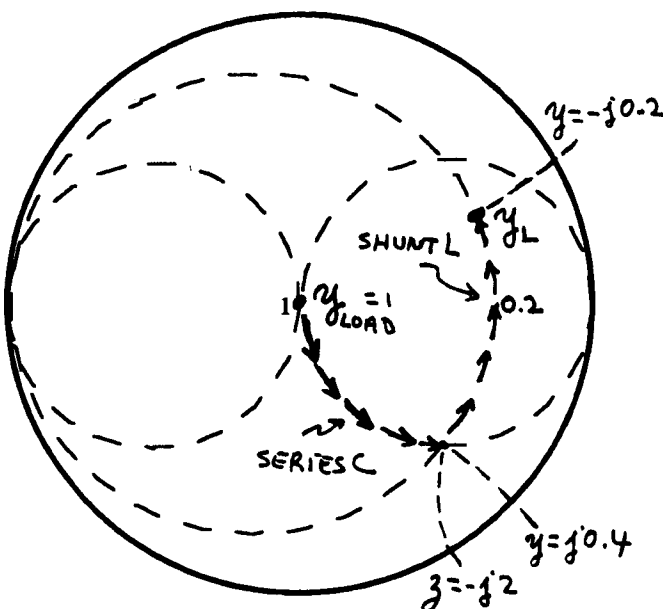
$$Z_C = 50 Z_C = -j60 \Omega$$

$$\text{SHUNT L: } Y_L = 0 - j2 = -j2$$

$$Z_L = \frac{50}{Y_L} = j25 \Omega$$



$$2.11) \quad Y_L = \frac{Y_L}{Y_0} = Z_0 Y_L = 50(4 - j4)10^{-3} = 0.2 - j0.2$$



$$\text{SERIES C: } Z_C = -j2 - j0 = -j2$$

$$Z_C = 50 Z_C = -j100 \Omega$$

$$\text{SHUNT L: } Y_L = -j0.2 - j0.4 = -j0.6$$

$$Z_L = \frac{50}{Y_L} = j83.3 \Omega$$

At $f = 700 \text{ MHz}$:

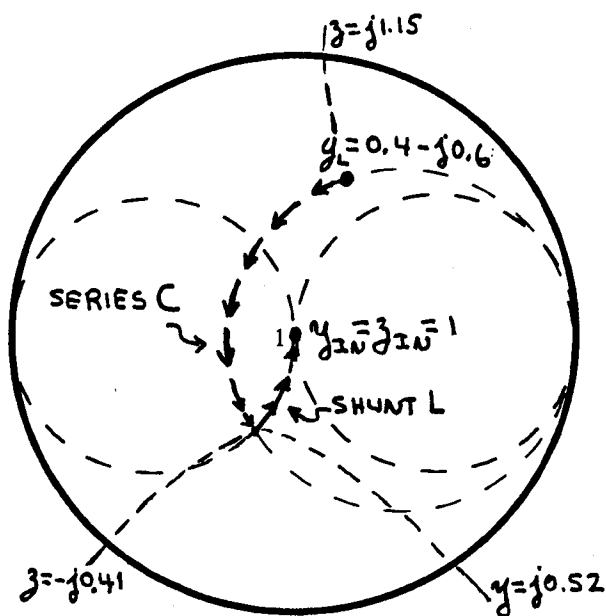
$$Z_L = j\omega L = j83.3$$

$$L = \frac{83.3}{2\pi 700 \cdot 10^6} = 18.9 \text{ nH}$$

$$Z_C = \frac{-j}{\omega C} = -j100$$

$$C = \frac{1}{100(2\pi 700 \cdot 10^6)} = 2.27 \text{ pF}$$

2.12) ONLY CIRCUIT (b) CAN MATCH $Y_L = 8 - j12 \text{ mS}$ to $Z_{IN} = 50 \Omega$.



$$\text{SERIES C: } Z_C = -j0.41 - j1.15 = -j1.56$$

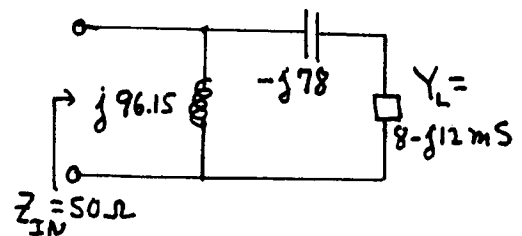
$$Z_C = 50 Z_C = -j78 \Omega$$

$$C = \frac{1}{\omega(78)} = \frac{1}{2\pi 10^9 (78)} = 2.04 \text{ pF}$$

$$\text{SHUNT L: } Y_L = 0 - j0.52 = -j0.52$$

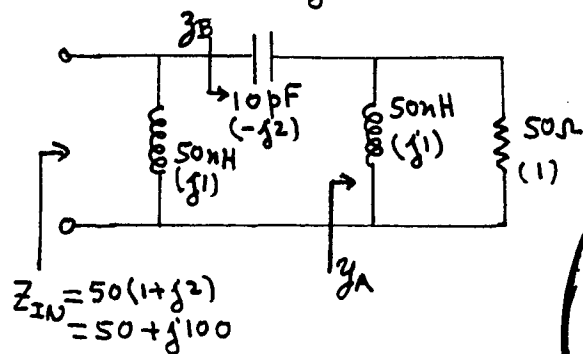
$$Z_L = \frac{50}{Y_L} = j96.15 \Omega$$

$$L = \frac{96.15}{\omega} = \frac{96.15}{2\pi 10^9} = 15.3 \text{ nH}$$



$$2.13) Z_L = j\omega L = j10^9 50 \cdot 10^{-9} = j50 \text{ OR } Z_L = j\frac{50}{50} = j1$$

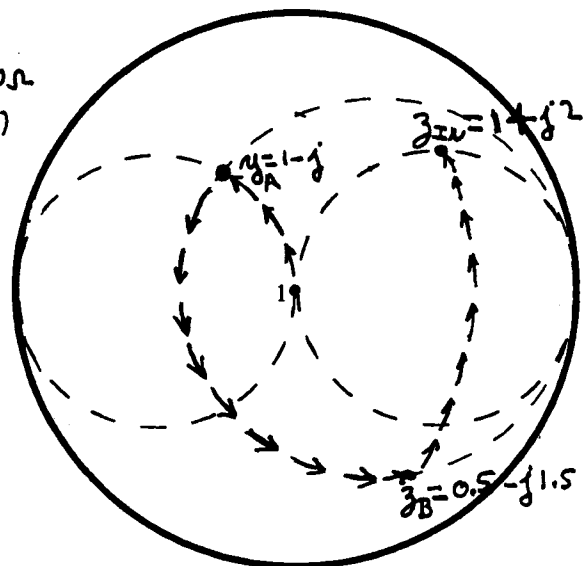
$$Z_C = \frac{1}{j\omega C} = \frac{1}{j10^9 10 \cdot 10^{-12}} = -j100 \text{ OR } Z_C = -j\frac{100}{50} = -j2$$



$$Z_{IN} = 50(1 + j2)$$

$$Z_{IN} = 50 + j100$$

$$Z_{IN} = 50 Z_{IN} = 50 + j100 \Omega$$



2.14) LET $Z_0 = 100 \Omega$.

THEN $z_L = \frac{Z_L}{100} = 1 - j$

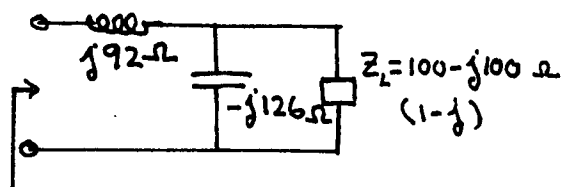
AND $z_{IN} = \frac{Z_{IN}}{100} = 0.25 + j0.25$

SHUNT C: $y_c = j1.31 - j0.5 = j1.26$

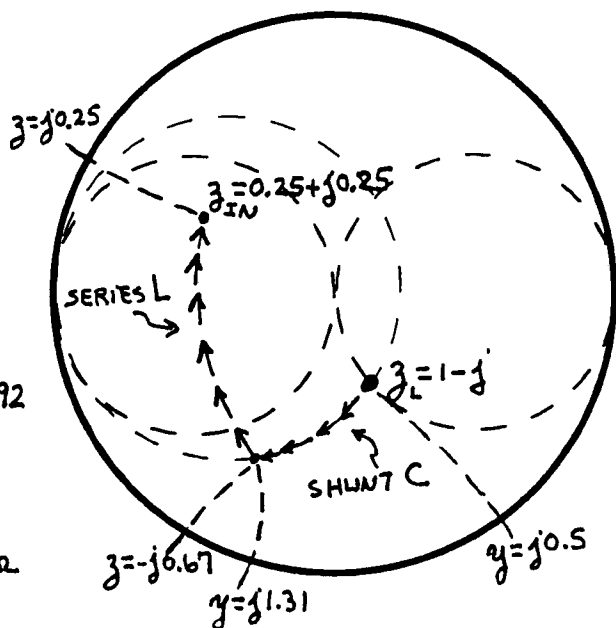
$Z_c = \frac{100}{y_c} = -j126 \Omega$

SERIES L: $z_L = j0.25 - (-j0.67) = j0.92$

$Z_L = 100 z_L = j92 \Omega$



$Z_{IN} = 25 + j25 \Omega$
($0.25 + j0.25$)



2.15) (a) $z_L = \frac{50}{50} = 1$

$z_{IN} = \frac{20 + j20}{50} = 0.4 + j0.4$

DRAW THE $Q=5$ CIRCLES (SEE FIG. 2.4.16)

THE MOTION FROM A TO B -- SERIES L_1 :

AT B: $z_B = 1 + j3$

$z_L = j3$ OR $Z_L = j3(50) = j150 \Omega$

THE MOTION FROM B TO C -- SHUNT C:

AT B: $y_B = 0.1 - j0.3$

AT C: $y_C = 0.1 + j0.5$

$y_c = j0.5 - (-j0.3) = j0.8$

$Z_c = \frac{50}{j0.8} = -j62.5 \Omega$

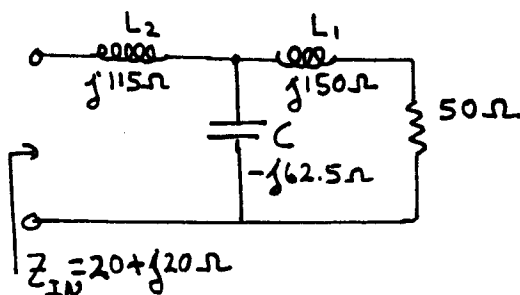
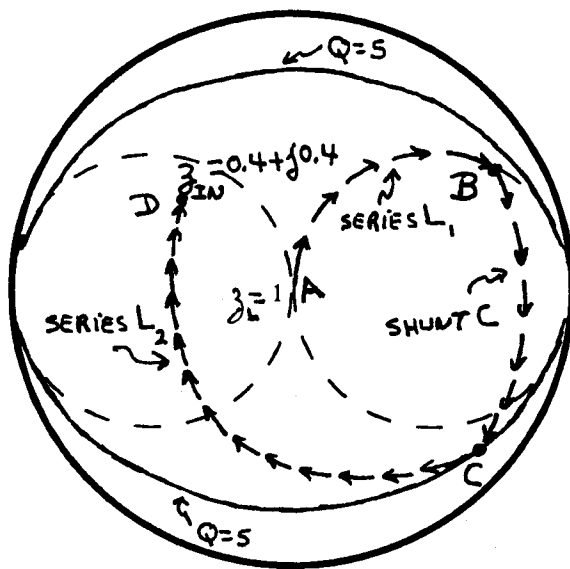
THE MOTION FROM C TO D -- SERIES L_2 :

AT C: $z_C = 0.4 - j1.9$

AT D: $z_D = 0.4 + j0.4$

$z_{L_2} = j0.4 - (-j1.9) = j2.3$

$Z_{L_2} = 50(j2.3) = j115 \Omega$



(b) $Z_L = 1$ AND $Z_{IN} = 0.5$

AT B: $y_B = 1 - j2.6$, $Z_B = 0.13 + j0.335$

AT C: $y_C = 2 - j3.4$, $Z_C = 0.13 + j0.215$

AT D: $y_D = 2$, $Z_D = Z_{IN} = 0.5$

SHUNT L: $y_L = -j2.6$

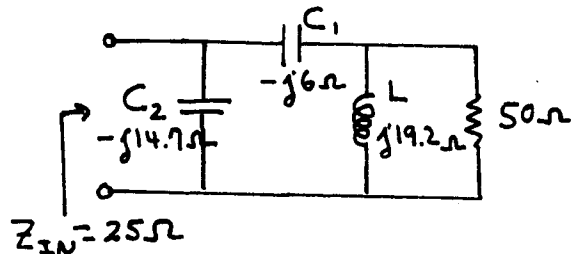
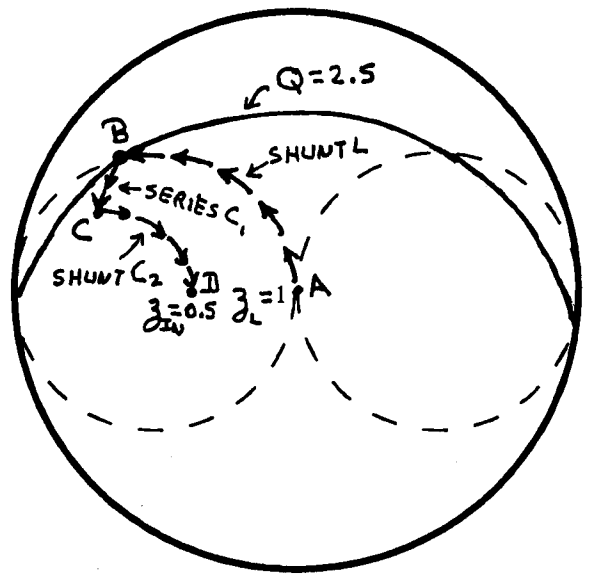
$$Z_L = \frac{50}{-j2.6} = j19.2 \Omega$$

SERIES C_1 : $Z_{C_1} = j0.215 - j0.335 = -j0.12$

$$Z_{C_1} = 50(-j0.12) = -j6 \Omega$$

SHUNT C_2 : $y_{C_2} = 0 - (-j3.4) = j3.4$

$$Z_{C_2} = \frac{50}{j3.4} = -j14.7 \Omega$$



2.16) (a) FROM FIG. 2.5.2 WITH $Z_0 = 50 \Omega$ AND $\epsilon_r = 2.23$ WE OBTAIN:

$$\frac{W}{h} \approx 3.1 \text{ OR } W = 3.1(0.7874) = 2.44 \text{ mm}$$

FROM FIG. 2.5.3 WITH $W/h = 3.1$ AND $\epsilon_r = 2.23$ WE OBTAIN:

$$\frac{\lambda}{\lambda_{TEM}} = 1.08 \text{ OR } \lambda = 1.08 \lambda_{TEM} = 1.08 \frac{\lambda_0}{\sqrt{2.23}} = 0.723 \lambda_0$$

SINCE $\lambda = \frac{\lambda_0}{\sqrt{\epsilon_{eff}}}$, THEN $\frac{1}{\sqrt{\epsilon_{eff}}} = 0.723$ OR $\epsilon_{eff} = 1.91$

(b) FROM (2.5.11): $\frac{W}{h} = \frac{2}{\pi} \left\{ B - 1 - \ln(2B-1) + \frac{2.23-1}{2(2.23)} \left[\ln(B-1) + 0.39 - \frac{0.61}{2.23} \right] \right\} \quad (1)$

WHERE $B = \frac{377\pi}{2(50)\sqrt{2.23}} = 7.931 \quad (2)$

SUBSTITUTE (2) INTO (1) TO OBTAIN: $\frac{W}{h} = 3.073$

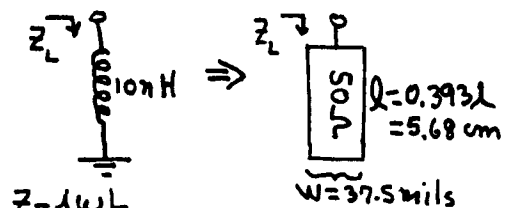
FROM (2.5.8): $\lambda = \frac{\lambda_0}{\sqrt{2.23}} \left[\frac{2.23}{1 + 0.63(2.23-1)(3.073)^{0.1255}} \right]^{1/2} = 0.724 \lambda_0$

$$\frac{1}{\sqrt{\epsilon_{eff}}} = 0.724 \text{ OR } \epsilon_{eff} = 1.91$$

2.17) APPROXIMATE VALUES CAN BE OBTAINED FROM FIGS. 2.5.2 AND 2.5.3.
EXACT VALUES ARE GIVEN IN FIG. 2.5.4.

$$\therefore \frac{W}{h} = 1.5 \text{ OR } W = 1.5(25) = 37.5 \text{ mils}$$

$$\text{FROM FIG. 2.5.3: } \frac{\lambda}{\lambda_{\text{TEM}}} = 1.18 \text{ OR } \lambda = 1.18 \lambda_{\text{TEM}} = \frac{1.18 \cdot 310^{10}}{\sqrt{6} \cdot 10^9} = 14.45 \text{ cm}$$



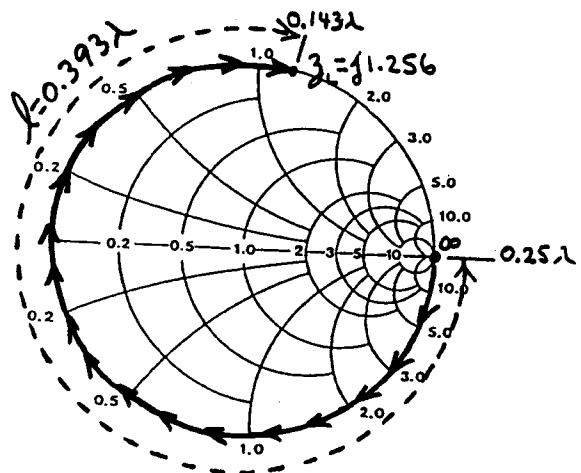
$$Z_L = j\omega L = j2\pi \cdot 10^9 \cdot 10^{-9} = j62.8\Omega$$

$$Z_L = \frac{Z_L}{50} = \frac{j62.8}{50} = j1.256$$

$$\text{HENCE: } l = 0.393\lambda$$

$$\text{OR } l = 0.393(14.45) = 5.68 \text{ cm}$$

$$\text{OR } l = 5.68 \left(\frac{1000}{2.54} \right) = 2,236.2 \text{ mils}$$



2.18) At $f = 1 \text{ GHz}$, $\lambda_0 = 30 \text{ cm}$. MICROSTRIP: $\epsilon_r = 2.23$, $h = 0.7874 \text{ mm}$

$$\text{LINE WITH } Z_0 = 29.9\Omega \text{ AND } l = \frac{\lambda}{4}: B = \frac{377\pi}{2(29.9)\sqrt{2.23}} = 13.26$$

$$\frac{W}{h} = \frac{2}{\pi} \left\{ 13.26 - 1 - \ln(2(13.26) - 1) + \frac{2.23 - 1}{2(2.23)} \left[\ln(13.26 - 1) + 0.39 - \frac{0.61}{2.23} \right] \right\} = 6.203$$

$$\therefore W = 6.203h = 6.203(0.7874) = 4.884 \text{ mm}$$

$$\lambda = \frac{\lambda_0}{\sqrt{2.23}} \left[\frac{2.23}{1 + 0.63(2.23 - 1)(6.203)^{0.1255}} \right]^{1/2} = 0.712\lambda_0$$

$$\text{NOTE: SINCE } \lambda = \frac{\lambda_0}{\sqrt{\epsilon_{\text{eff}}}} \text{ THEN } \frac{1}{\sqrt{\epsilon_{\text{eff}}}} = 0.712 \text{ OR } \epsilon_{\text{eff}} = 1.974$$

$$l = \frac{\lambda}{4} = 0.25(0.712\lambda_0) = 0.25(0.712)(30) = 5.34 \text{ cm}$$

SIMILARLY, WE OBTAINED:

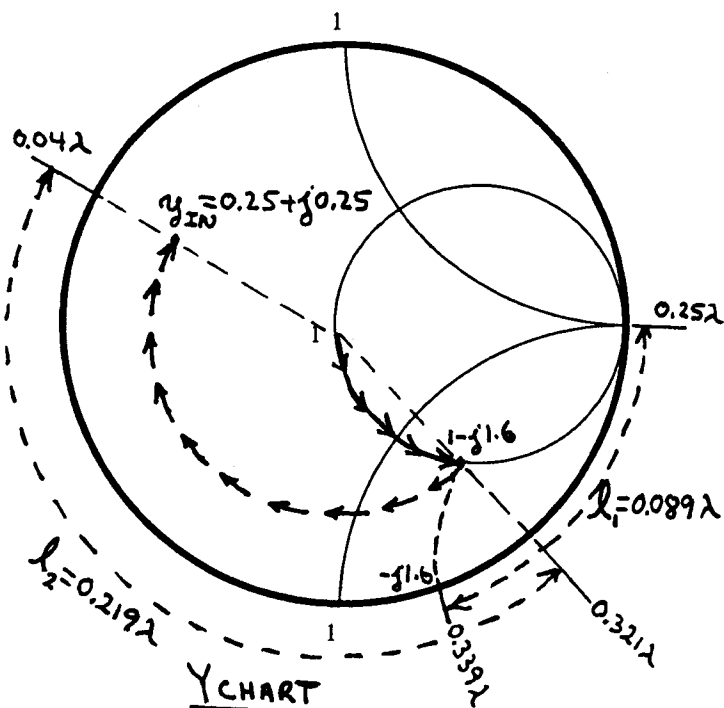
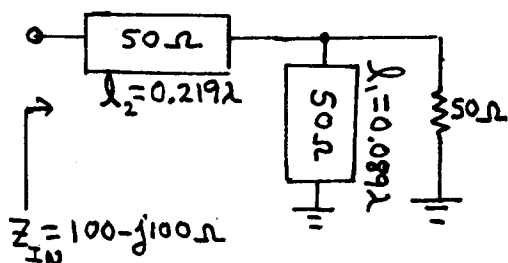
$Z_0 = 52.64\Omega, l = 3\lambda/8$	$Z_0 = 95.2\Omega, l = 3\lambda/8$	$Z_0 = 79\Omega, l = \lambda/4$
$\frac{W}{h} = 2.89 \text{ OR } W = 2.27 \text{ mm}$	$\frac{W}{h} = 0.99, W = 0.779 \text{ mm}$	$\frac{W}{h} = 1.44, W = 1.134 \text{ mm}$
$\lambda = 0.726\lambda_0, \epsilon_{\text{eff}} = 1.89$	$\lambda = 0.747\lambda_0, \epsilon_{\text{eff}} = 1.79$	$\lambda = 0.74\lambda_0, \epsilon_{\text{eff}} = 1.825$
$l = \frac{3\lambda}{8} = \frac{3}{8}(0.726)(30) = 8.167 \text{ cm}$	$l = \frac{3\lambda}{8} = 8.4 \text{ cm}$	$l = \frac{\lambda}{4} = 5.55 \text{ cm}$

2.19) (a) $z_{IN} = \frac{Z_{IN}}{50} = 2 - j2$

$y_{IN} = \frac{1}{z_{IN}} = 0.25 + j0.25$

$l_1 = 0.339\lambda - 0.25\lambda = 0.089\lambda$

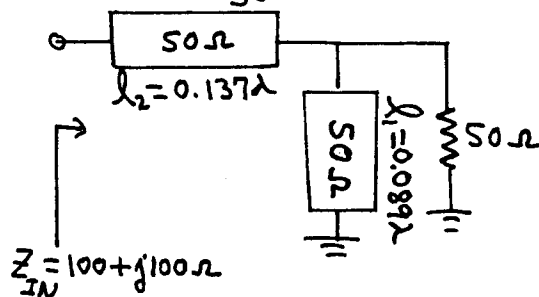
$l_2 = 0.04\lambda + (0.5\lambda - 0.321\lambda) = 0.219\lambda$



(b) If l_1 is an OPEN-CIRCUITED STUB, THEN

$l_1 = 0.25\lambda + 0.089\lambda = 0.339\lambda$

(c) For $z_{IN} = \frac{Z_{IN}}{50} = 2 + j2$, ONE ANSWER IS:



IF l_1 is an OPEN-CIRCUITED STUB, THEN

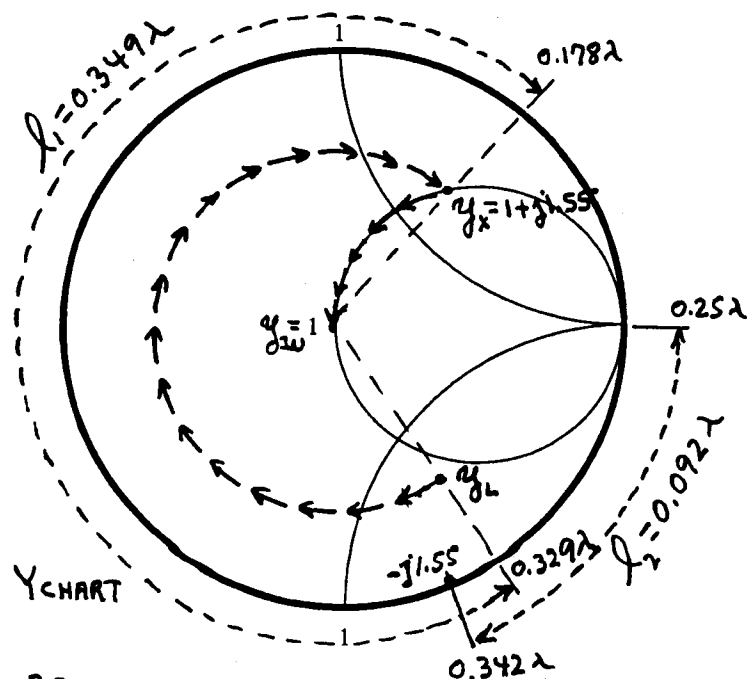
$l_1 = 0.25\lambda + 0.089\lambda = 0.339\lambda$

2.20) (a) $z_L = \frac{15 + j25}{50} = 0.3 + j0.5$
 $y_L = \frac{1}{z_L} = 0.882 - j1.47$

ROTATE, ALONG A CONSTANT $|S|$ CIRCLE, FROM y_L UNTIL THE UNIT CONDUCTANCE CIRCLE IS REACHED AT y_x .

$y_x = 1 + j1.55$

$l_1 = 0.178\lambda + (0.5\lambda - 0.329\lambda) = 0.349\lambda$



$$y_{IN} = y_{s.c} + y_x$$

$$1 = y_{s.c} + (1 + j1.55)$$

HENCE, $y_{s.c} = -j1.55$

THE LENGTH l_2 OF THE SHORT CIRCUITED STUB MUST HAVE

$$y_{s.c} = -j1.55$$

FROM THE Y SMITH CHART:

$$l_2 = 0.342\lambda - 0.25\lambda = 0.092\lambda$$

(b) IF THE CHARACTERISTIC IMPEDANCE OF THE STUB IS $Z'_0 = 100 \Omega$.

$$Z_{s.c.} = \frac{50}{y_{s.c}} = \frac{50}{-j1.55} = j32.26 \Omega$$

THEN: $j32.26 = jZ'_0 \tan \beta d = j100 \tan \beta d \Rightarrow \beta d = 0.312$

$$d = l_2 = \frac{0.312}{2\pi/\lambda} = 0.05\lambda$$

ANOTHER WAY: NORMALIZE $Z_{s.c.}$ WITH Z'_0 , $z_{s.c.} = \frac{j32.26}{100} = j0.323$

THEN: $y_{s.c.} = \frac{1}{z_{s.c.}} = -j3.09$. LOCATE $y_{s.c.} = -j3.09$ IN THE Y SMITH CHART, AND READ $l_2 = 0.302\lambda - 0.25\lambda = 0.052\lambda$

2.21) (a) $Y_{IN} = G_{IN} + jB_{IN} = 50 + j40 \text{ mS}$, $R_{IN} = \frac{1}{G_{IN}} = \frac{1}{50 \times 10^{-3}} = 20 \Omega$

$$Z_{01} = \sqrt{Z_L R_{IN}} = \sqrt{50(20)} = 31.62 \Omega$$

IN A SHORT-CIRCUITED $\frac{3\lambda}{8}$ STUB: $Y_{s.c.} = jY_{02}$. HENCE, $jY_{02} = jB_{IN} = j40 \text{ mS}$

OR $Y_{02} = 40 \text{ mS}$, $Z_{02} = \frac{1}{Y_{02}} = 25 \Omega$

(b) $Y_{IN} = G_{IN} - jB_{IN} = 50 - j40 \text{ mS}$, $R_{IN} = \frac{1}{G_{IN}} = 20 \Omega$.

THEN, $Z_{01} = \sqrt{50(20)} = 31.62 \Omega$. IN A SHORT-CIRCUITED $\frac{\lambda}{8}$ STUB:

$Y_{s.c.} = -jY_{02}$. HENCE, $Y_{02} = 40 \text{ mS}$ OR $Z_{02} = \frac{1}{40 \times 10^{-3}} = 25 \Omega$.

(c) $Y_{IN} = G_{IN} + jB_{IN} = 10 + j20 \text{ mS}$, $R_{IN} = \frac{1}{G_{IN}} = \frac{1}{10 \times 10^{-3}} = 100 \Omega$

THEN, $Z_{01} = \sqrt{50(100)} = 70.7 \Omega$. IN AN OPEN-CIRCUITED $\frac{\lambda}{8}$ STUB:

$Y_{o.c.} = jY_{02}$. HENCE, $Y_{02} = 20 \text{ mS}$ OR $Z_{02} = \frac{1}{20 \times 10^{-3}} = 50 \Omega$.

(d) $Y_{IN} = 10 - j20 \text{ mS}$. HENCE: $Z_{01} = \sqrt{50(100)} = 70.7 \Omega$.

IN AN OPEN-CIRCUITED $\frac{3\lambda}{8}$ STUB: $Y_{o.c.} = -jY_{02}$. HENCE, $Z_{02} = \frac{1}{Y_{02}} = \frac{1}{20 \times 10^{-3}} = 50 \Omega$.

2.22) (a) $\Gamma_2 = 0.5 \angle 90^\circ$, $Z_2 = 0.6 + j0.8$

$$\therefore y_2 = \frac{1}{z_2} = 0.6 - j0.8$$

FROM THE SMITH CHART:

$$\lambda_1 = 0.136\lambda, \lambda_2 = 0.375\lambda - 0.166\lambda = 0.209\lambda$$

IN FIG. P.22(b):

$$Y_2 = \frac{0.6 - j0.8}{50} = 12 - j16 \text{ mS}$$

$$\therefore Z_{01} = \sqrt{50 \left(\frac{1}{12 \times 10^3} \right)} = 64.5 \, \Omega$$

USING A $\frac{3\lambda}{8}$ OPEN-CIRCUITED STUB:

$$-jY_{02} = -j16 \text{ mS}, \text{ or } Y_{02} = 16 \text{ mS}$$

$$Z_{02} = \frac{1}{16 \times 10^{-3}} = 62.5 \Omega$$

(b) BALANCED FORM OF THE STUBS.

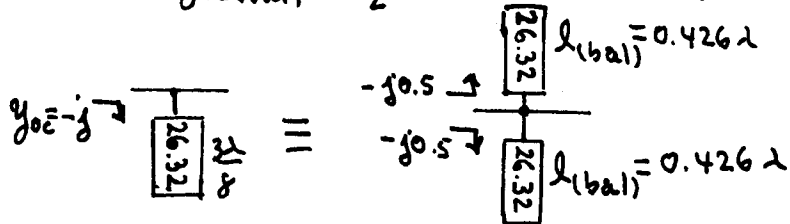
For Fig. P.22(a): $y_{bal} = f \frac{1.15}{2} = f 0.575 \Rightarrow l_{1(bal)} = 0.0832$

FOR FIG. P. 22(b): $Z_{O2(bal)} = 2(62.5) = 125 \Omega$

2.23) THE $\frac{3\lambda}{8}$ STUB WITH $Z_0 = 26.32\Omega$ HAS AN ADMITTANCE OF $-j0.038S$.

IN A $Z_0 = 26.32 \Omega$ SYSTEM: $y_{oc} = (26.32)(-j0.038) = -j1$

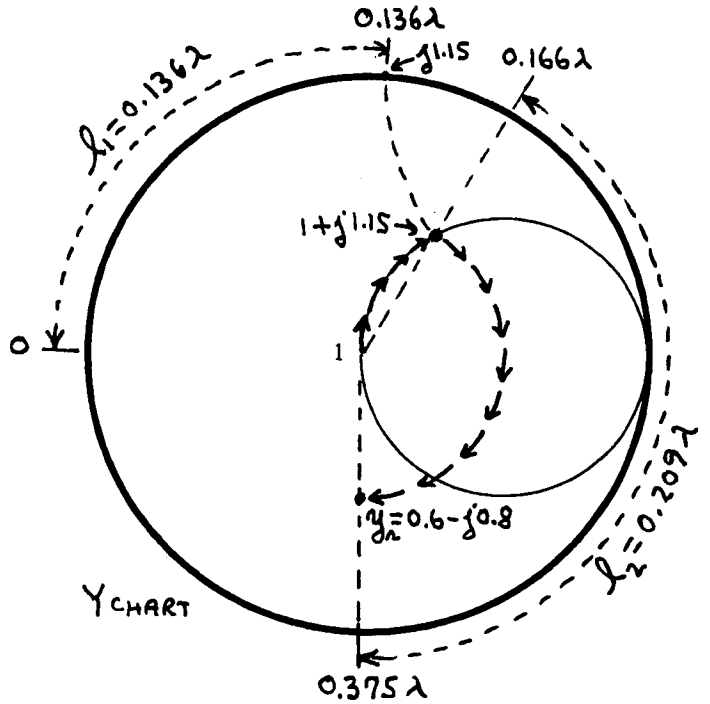
Then: $y_{loc(bal)} = \frac{-j1}{2} = -j0.5 \Rightarrow l_{(bal)} = 0.426 \lambda$



THE $3\lambda/8$ STUB WITH $Z_0 = 47.6 \Omega$ HAS AN ADMITTANCE OF $-j0.021 S$.

$$y_{oc} = 47.6(-j0.021) = -j1$$

THEN: $y_{oc(bal)} = -f \frac{1}{2} = -f 0.5 \Rightarrow l_{(bal)} = 0.426 \lambda$

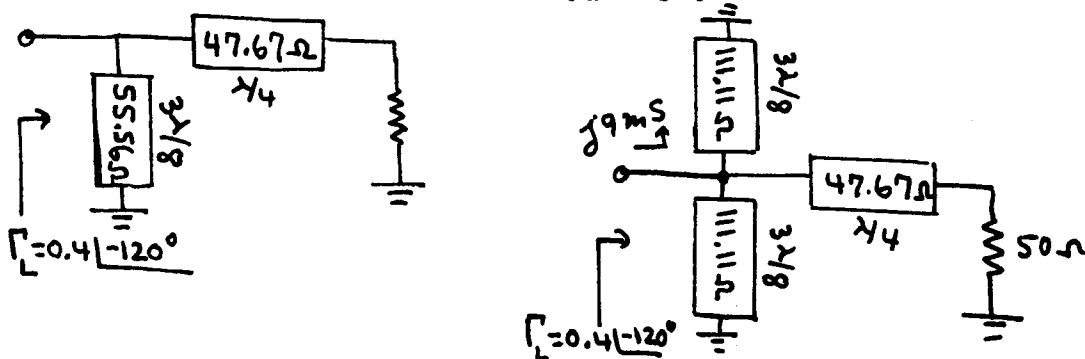


2.24) (a) $\Gamma_L = 0.4 \angle -120^\circ$, $Z_L = 0.538 - j0.444$, $y_L = \frac{1}{Z_L} = 1.105 + j0.912$

$Y_L = \frac{y_L}{50} = 22 + j18 \text{ mS}$

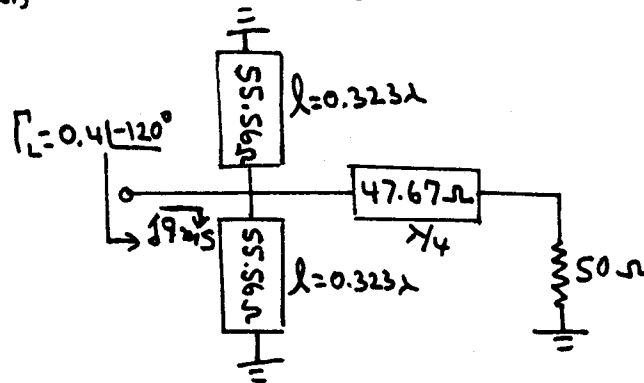
HENCE: $Z_{01} = \sqrt{50 \left(\frac{1}{22 \times 10^{-3}} \right)} = 47.67 \Omega$ AND

$jY_{02} = j18 \text{ mS}$ OR $Z_{02} = \frac{1}{Y_{02}} = \frac{1}{18 \times 10^{-3}} = 55.56 \Omega$



BALANCE FORM (USE $2Z_{02} = 111.11 \Omega$)

(b) EACH SIDE OF THE BALANCE STUBS HAS AN ADMITTANCE OF $j9 \text{ mS}$. IF ITS CHARACTERISTIC IMPEDANCE IS $Z_0 = \frac{111.11}{2} = 55.56 \Omega$, THEN $y_{(bal)} = j9 \times 10^{-3} (55.56) = j0.5$. HENCE: $l = 0.323 \lambda$.



2.25) $\Gamma_L = 0.8 \angle 160^\circ$, $y_L = \frac{1}{Z_L} = 2.64 - j4$

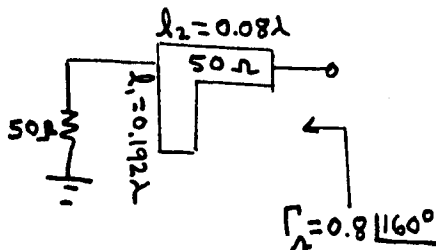
$\Gamma_L = 0.7 \angle 20^\circ$, $y_L = \frac{1}{Z_L} = 0.182 - j0.171$

THE DESIGN OF THE MATCHING CIRCUITS IS SHOWN IN THE Γ SMITH CHARTS.

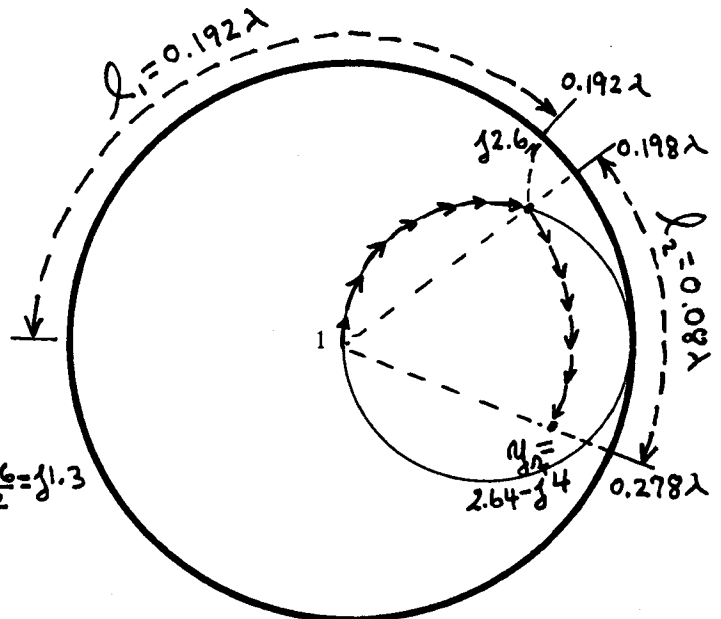
MATCHING TO Γ_L :

OPEN STUB LENGTH: $l_1 = 0.192\lambda$

SERIES TRANS. LINE: $l_2 = 0.08\lambda$



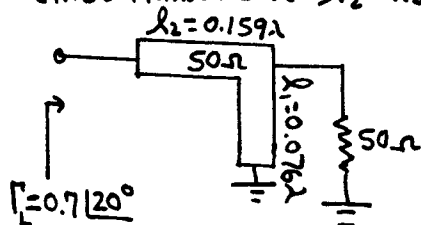
BALANCED SHUNT STUBS: $y_{(b2)} = j \frac{2.6}{2} = j1.3$
 LENGTH OF EACH SIDE: $l'_1 = 0.146\lambda$



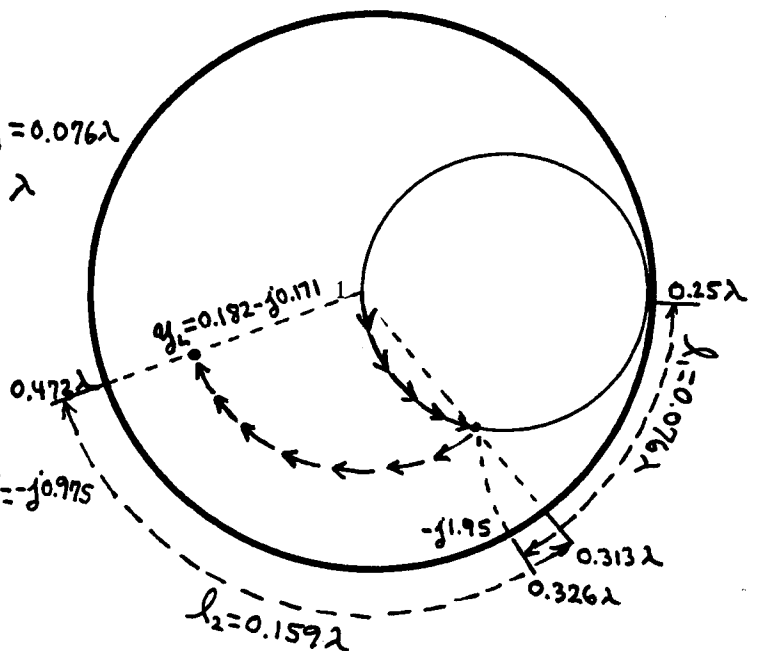
MATCHING TO Γ_L :

SHORT-CIRCUITED STUB LENGTH: $l_1 = 0.076\lambda$

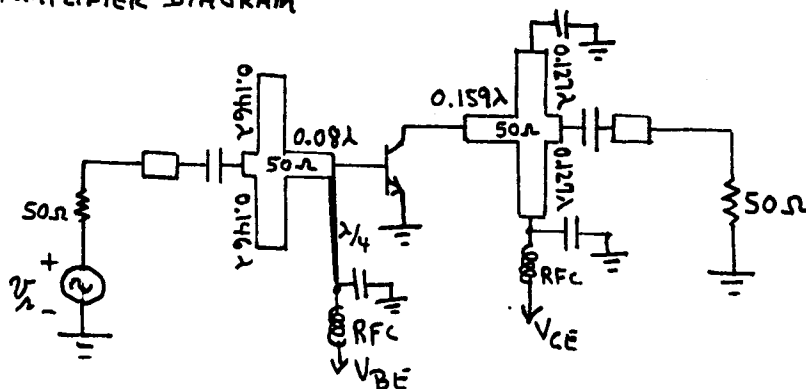
SERIES TRANS. LINE: $l_2 = 0.159\lambda$



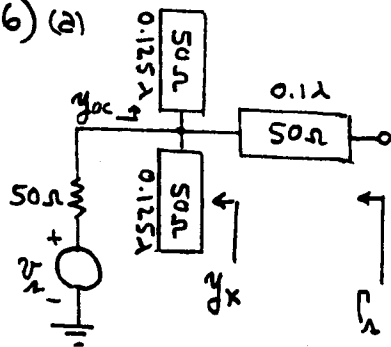
BALANCED SHUNT STUBS: $y_{(b2)} = -j \frac{1.95}{2} = -j0.975$
 LENGTH OF EACH SIDE: $l'_1 = 0.127\lambda$



AMPLIFIER DIAGRAM



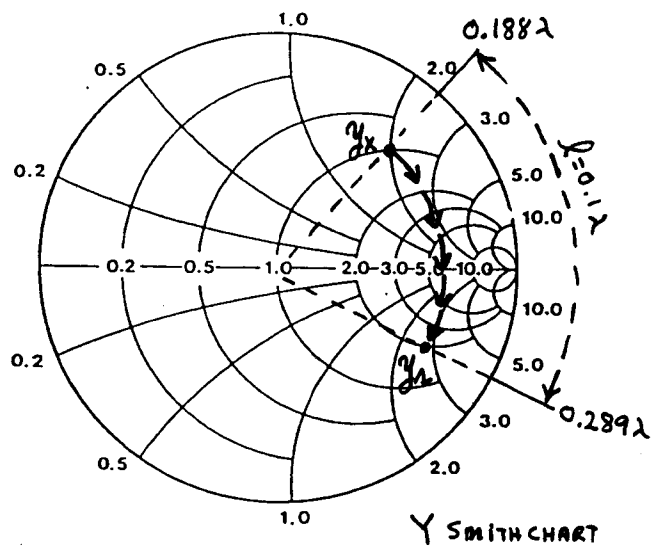
2.26) (a)



THE ADMITTANCE OF THE 0.125 λ STUB

IS: $y_{oc} = j$

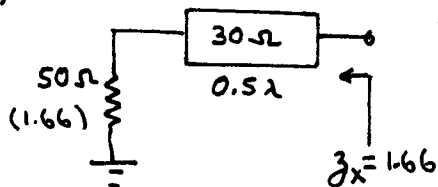
HENCE: $y_x = 1 + j + j = 1 + 2j$



LOCATE y_x IN THE Y CHART, AND ROTATE 0.1 λ TO FIND y_2 . HENCE

$y_2 = 2 - j2.7$ AND $\Gamma_2 = 0.71 \angle 152^\circ$

(b)



NORMALIZING WITH $Z_0 = 30 \Omega$

$z = \frac{50}{30} = 1.66$

HENCE, THE IMPEDANCE z_x AT 0.5 λ FROM THE LOAD END IS:

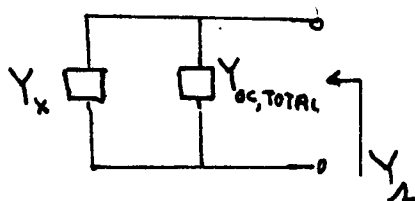
$z_x = 1.66$ OR $Z_x = 30(1.66) = 50 \Omega$

AND $Y_x = \frac{1}{Z_x} = 20 \text{ mS}$

THE 75 Ω , 0.46 λ BALANCE STUB HAS: $y_{oc} = -j0.26$ OR

$y_{oc, \text{TOTAL}} = 2(-j0.26) = -j0.52$

$Y_{oc, \text{TOTAL}} = -j \frac{0.52}{75} = -j7 \text{ mS}$



$Y_2 = Y_x + Y_{oc, \text{TOTAL}}$

$Y_2 = 20 - j7 \text{ mS}$

IN A 50- Ω SYSTEM: $y_2 = 50 Y_2 = 1 - j0.35$

$z_2 = \frac{1}{y_2} = 0.891 + j0.312$

AND $\Gamma_2 = 0.172 \angle 99.9^\circ$

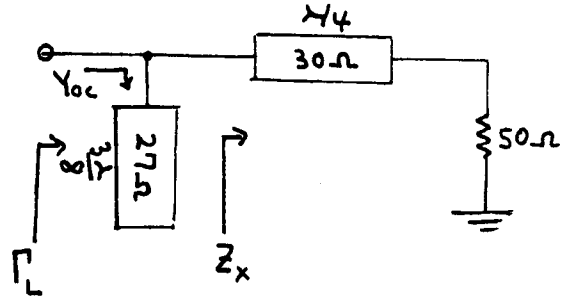
$$2.27)(a) \lambda = \frac{3 \cdot 10^{10}}{6 \cdot 10^9} = 5 \text{ cm}, \quad l_1 = 1.25 \text{ cm} = 1.25 \frac{\lambda}{5} = \frac{\lambda}{4}$$

$$l_2 = 1.87 \text{ cm} = 1.87 \frac{\lambda}{5} = 0.375 \lambda = \frac{3\lambda}{8}$$

FOR THE $\frac{\lambda}{4}$ LINE:

$$Z_x = \frac{Z_0^2}{Z_L} = \frac{30^2}{50} = 18 \Omega$$

$$Y_x = \frac{1}{Z_x} = 56 \text{ mS}$$



FOR THE $\frac{3\lambda}{8}$ STUB:

$$y_{0c} = -j, \quad Y_{0c} = \frac{1}{27}(-j) = -j37 \text{ mS}$$

$$\text{HENCE: } Y_L = Y_x + Y_{0c} = 56 - j37 \text{ mS}$$

$$\text{IN A } 50 \Omega \text{ SYSTEM: } y_L = 50 Y_L = 2.8 - j1.85 \text{ AND } \Gamma_L = 0.61 \angle 160.2^\circ$$

(b) FOR BALANCE STUBS USE $Z_0 = 2(27) = 54 \Omega$ WITH LENGTHS OF $3\frac{\lambda}{8}$.

$$2.28) \Gamma_{IN} = 0.5 \angle 100^\circ, \quad z_{IN} = 0.527 + j0.692$$

THE $50 \Omega, 0.15\lambda$ TRANSFORMS z_{IN} TO THE IMPEDANCE $z_x = 2.94 - j0.74$,

$$\text{OR } y_x = \frac{1}{z_x} = 0.32 + j0.08$$

THE ADMITTANCE OF THE $\frac{\lambda}{8}$ STUB IS: $y_{0c} = j$. HENCE, FOR THE

$$\text{TWO STUBS: } y_{0c, \text{TOTAL}} = j + j = 2j$$

$$\text{THEN, } y_A = y_x + y_{0c, \text{TOTAL}} = 0.32 + j0.08 + j2 = 0.32 + j2.08$$

$$Z_A = 50 z_A = \frac{50}{y_A} = (0.072 - j0.47)50 = 3.6 - j23.5 \Omega$$

2.29)

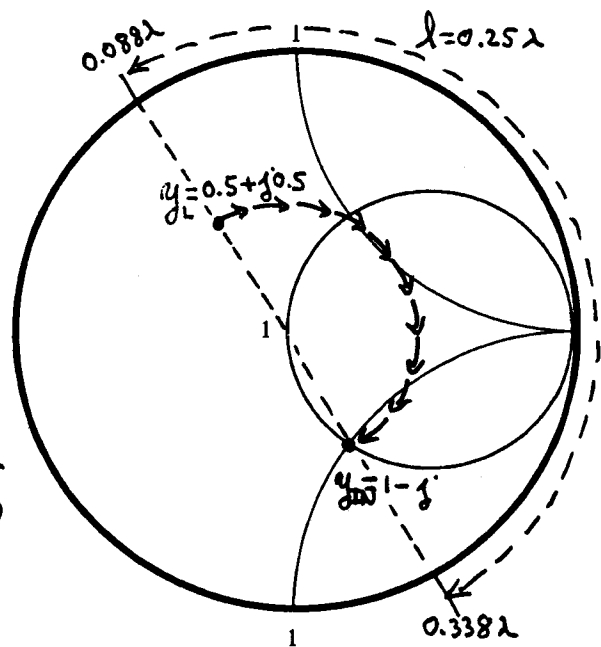
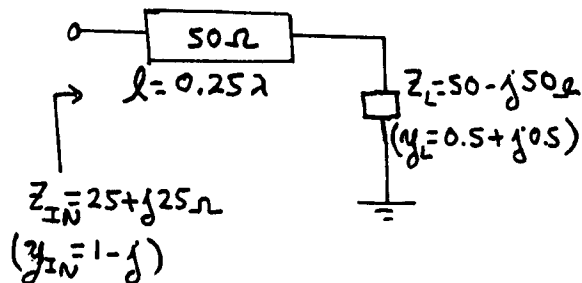
$$z_L = \frac{Z_L}{50} = 1 - j, \quad z_{IN} = \frac{Z_{IN}}{50} = 0.5 + j0.5$$

$$y_L = \frac{1}{z_L} = 0.5 + j0.5, \quad y_{IN} = \frac{1}{z_{IN}} = 1 - j$$

y_L AND y_{IN} ARE ON THE SAME CONSTANT $|\Gamma|$ CIRCLE. HENCE, A SERIES TRANSMISSION LINE OF LENGTH:

$$l = 0.338\lambda - 0.088\lambda = 0.25\lambda$$

WILL CHANGE y_L TO y_{IN} .



2.30) $z_L = \frac{50 + j50}{50} = 1 + j$

THE 50Ω , 0.125λ CHANGES $z_L = 1 + j$ TO $z_x = 2 - j$ (OR $y_x = 0.4 + j0.2$)

THE 50Ω , 0.125λ STUB HAS: $y_{oc} = j$

HENCE: $y_L = y_x + y_{oc} = 0.4 + j0.2 + j = 0.4 + j1.2$ AND $\Gamma_L = 0.728 \angle -104^\circ$

2.31) LOCATE $\Gamma_n = 0.57 \angle 116^\circ$ IN

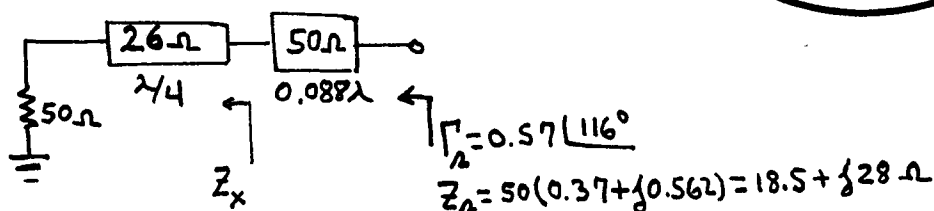
THE SMITH CHART AND READ:

$$z_x = 0.27 \text{ OR } Z_x = 50z_x = 13.5\Omega$$

THE TRANSFORMATION OF 50Ω TO $Z_x = 13.5\Omega$ CAN BE DONE WITH A $\frac{\lambda}{4}$ LINE WITH: $Z_0 = \sqrt{50(13.5)} = 26\Omega$

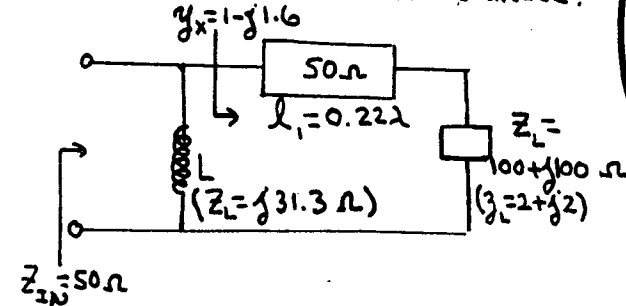
THEN, A SERIES TRANS. LINE OF LENGTH: $l = 0.088\lambda$ TRANSFORMS

$Z_x = 13.5\Omega$ TO $Z_n = 18.5 + j28\Omega$ OR $\Gamma_n = 0.57 \angle 116^\circ$

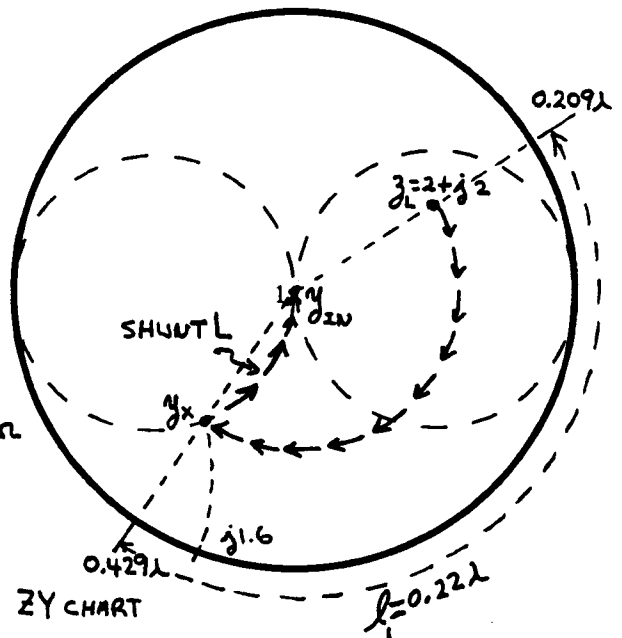


$$2.32) (a) \quad z_L = \frac{100 + j100}{50} = 2 + j2$$

THE TRANSMISSION LINE PRODUCES A MOTION ALONG A CONSTANT $|r|$ CIRCLE, AND THE INDUCTOR L PRODUCES A MOTION ALONG A CONSTANT CONDUCTANCE CIRCLE.



USING A ZY SMITH CHART:
 $l_1 = 0.429\lambda - 0.209\lambda = 0.22\lambda$



AT y_x : $y_x = 1 - j1.6$. THEN, $y_L = 0 - (j1.6) = -j1.6$
 OR $Z_L = 50 z_L = \frac{50}{-j1.6} = j31.3 \Omega$

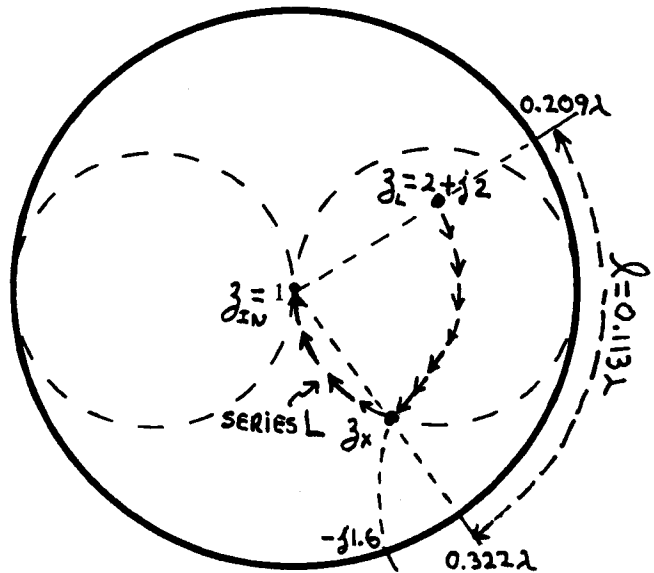
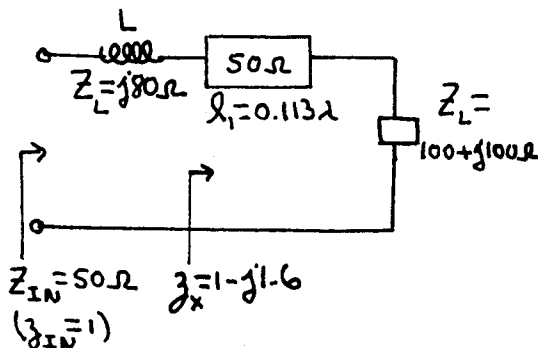
(b) IN THIS CIRCUIT THE INDUCTOR PRODUCES A MOTION ALONG A CONSTANT RESISTANCE CIRCLE.

$$l_1 = 0.322\lambda - 0.209\lambda = 0.113\lambda$$

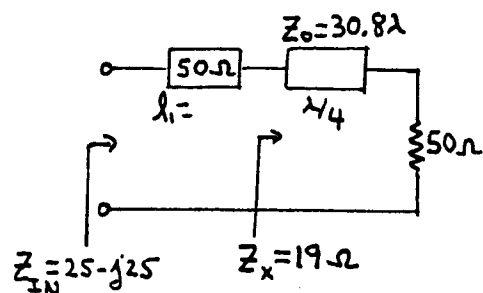
$$\text{AT } z_x: z_x = 1 - j1.6$$

$$z_L = 0 - (-j1.6) = j1.6$$

$$Z_L = 50 z_L = 50(j1.6) = j80 \Omega$$



2.33) (a) $z_{IN} = \frac{25 - j25}{50} = 0.5 - j0.5$

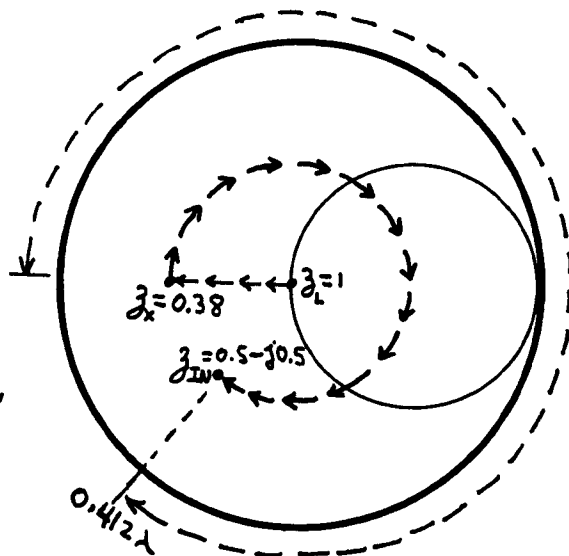


Z_x AND Z_{IN} MUST BE ON THE SAME CONSTANT $|P|$ CIRCLE. ONE SOLUTION IS SHOWN ON THE SMITH CHART.

$$Z_x = 50z_L = 50(0.38) = 19\Omega$$

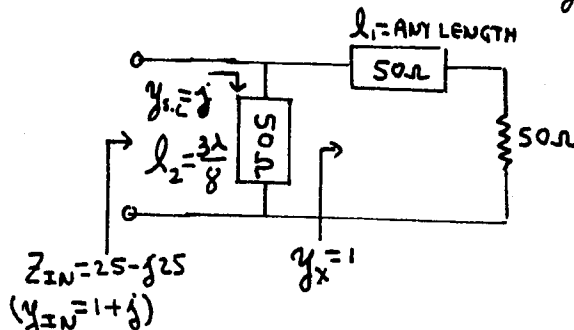
THEN: $Z_o = \sqrt{Z_L Z_x} = \sqrt{50(19)} = 30.8\Omega$

AND $l_1 = 0.412\lambda$



(b) $z_{IN} = 0.5 - j0.5$, $y_{IN} = \frac{1}{z_{IN}} = 1 + j$

LETTING $Z_o = 50\Omega$ AND $l_1 = \text{ANY LENGTH}$, THE ADMITTANCE $y_x = 1$. THEN, THE SHUNT STUB MUST PROVIDE: $y_{s.c} = j$. HENCE: $l_2 = \frac{3\lambda}{8}$.

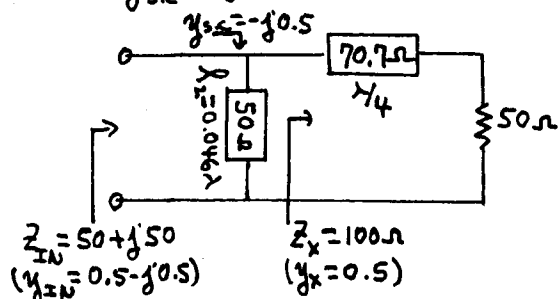


$$y_{IN} = y_x + y_{s.c} = 1 + j$$

(c) $z_{IN} = \frac{50 + j50}{50} = 1 + j$, $y_{IN} = 0.5 - j0.5$, $Y_{IN} = 10 - j10 \text{ mS}$

$\therefore Z_o = \sqrt{Z_L Z_x} = \sqrt{50(\frac{1}{10 \cdot 10^{-3}})} = 70.7\Omega$. THE STUB ADMITTANCE MUST

BE: $y_{s.c} = -j0.5$. HENCE: $l_2 = 0.426\lambda$



$$y_{IN} = y_x + y_{s.c} = 0.5 - j0.5$$

2.34) STARTING WITH (2.6.13):

$$G_T = \frac{(1-|\Gamma_L|^2) |S_{21}|^2 (1-|\Gamma_L|^2)}{|(1-S_{11}\Gamma_L)(1-S_{22}\Gamma_L) - S_{21}S_{12}\Gamma_L\Gamma_L|^2} \quad (1)$$

THE DENOMINATOR CAN BE EXPRESSED AS

$$\begin{aligned} |1-S_{22}\Gamma_L|^2 \left| 1 - \frac{S_{11}\Gamma_L - S_{12}S_{21}\Gamma_L\Gamma_L}{1-S_{22}\Gamma_L} \right|^2 &= \\ |1-S_{22}\Gamma_L|^2 \left| 1 - \Gamma_L \left(\frac{S_{11} - S_{12}S_{21}\Gamma_L}{1-S_{22}\Gamma_L} \right) \right|^2 &= |1-S_{22}\Gamma_L|^2 |1-\Gamma_L\Gamma_{IN}|^2 \end{aligned}$$

HENCE, (1) CAN BE EXPRESSED IN THE FORM

$$G_T = \frac{1-|\Gamma_L|^2}{|1-\Gamma_L\Gamma_{IN}|^2} |S_{21}|^2 \frac{1-|\Gamma_L|^2}{|1-S_{22}\Gamma_L|^2} \quad (2.6.14)$$

ANOTHER WAY OF WRITING THE DENOMINATOR IS:

$$\begin{aligned} |1-S_{11}\Gamma_L|^2 \left| 1 - \frac{S_{22}\Gamma_L - \frac{S_{12}S_{21}\Gamma_L\Gamma_L}{1-S_{11}\Gamma_L}}{1-S_{11}\Gamma_L} \right|^2 &= \\ |1-S_{11}\Gamma_L|^2 \left| 1 - \Gamma_L \left(\frac{S_{22} - \frac{S_{12}S_{21}\Gamma_L}{1-S_{11}\Gamma_L}}{1-S_{11}\Gamma_L} \right) \right|^2 &= |1-S_{11}\Gamma_L|^2 |1-\Gamma_L\Gamma_{OUT}|^2 \end{aligned}$$

HENCE, (1) CAN ALSO BE EXPRESSED AS:

$$G_T = \frac{1-|\Gamma_L|^2}{|1-S_{11}\Gamma_L|^2} |S_{21}|^2 \frac{1-|\Gamma_L|^2}{|1-\Gamma_L\Gamma_{OUT}|^2} \quad (2.6.15)$$

$$2.35) \frac{b_1}{b_L} = \frac{S_{11}(1-\Gamma_L S_{22}) + S_{21}\Gamma_L S_{12}}{D}, \quad \frac{b_2}{b_L} = \frac{S_{21}}{D}$$

$$\frac{a_1}{b_L} = \frac{1-S_{22}\Gamma_L}{D}, \quad \frac{a_2}{b_L} = \frac{S_{21}\Gamma_L}{D},$$

$$D = 1 - (S_{11}\Gamma_L + S_{22}\Gamma_L + S_{21}\Gamma_L S_{12}\Gamma_L) + S_{11}\Gamma_L S_{22}\Gamma_L$$

$$\begin{aligned} \text{Hence: } A_v &= \frac{\frac{a_2}{b_L} + \frac{b_2}{b_L}}{\frac{a_1}{b_L} + \frac{b_1}{b_L}} = \frac{S_{21}\Gamma_L + S_{21}}{S_{11}(1-\Gamma_L S_{22}) + S_{21}\Gamma_L S_{12} + 1 - S_{22}\Gamma_L} \\ \text{OR } A_v &= \frac{S_{21}(\Gamma_L + 1)}{1 - S_{22}\Gamma_L + S_{11}(1-\Gamma_L S_{22}) + S_{21}\Gamma_L S_{12}} \end{aligned}$$

2.36) (a) From (2.8.6), with $\Gamma_L = \Gamma_{out}^* = 0.682 \angle 97^\circ$, we obtain $|\Gamma_b| = 0$.

Then, using (2.8.4), $(VSWR)_{out} = 1$.

(b) When $\Gamma_L = \Gamma_{out}^*$ we have $|\Gamma_b| = 0$ or $\Gamma_b = 0$. Hence,
 $Z_b = Z_0 = 50 \Omega$.

$$(c) \quad |\Gamma_b| = \left| \frac{\Gamma_{out} - \Gamma_L^*}{1 - \Gamma_{out} \Gamma_L} \right| = \left| \frac{0.5 \angle -60^\circ - 0.682 \angle -97^\circ}{1 - 0.5 \angle -60^\circ (0.682 \angle 97^\circ)} \right| = 0.546$$

$$(VSWR)_{out} = \frac{1 + 0.546}{1 - 0.546} = 3.41$$

2.37) (a) From (2.8.3), with $\Gamma_L = \Gamma_{in}^* = 0.545 \angle 77.7^\circ$, we obtain $|\Gamma_a| = 0$.

Then, using (2.8.1), $(VSWR)_{in} = 1$.

(b) When $\Gamma_L = \Gamma_{in}^*$ we have $|\Gamma_a| = 0$ or $\Gamma_a = 0$. Hence,
 $Z_a = Z_0 = 50 \Omega$

$$(c) \quad |\Gamma_a| = \left| \frac{\Gamma_{in} - \Gamma_L^*}{1 - \Gamma_{in} \Gamma_L} \right| = \left| \frac{0.4 \angle 45^\circ - 0.545 \angle -77.7^\circ}{1 - 0.4 \angle 45^\circ (0.545 \angle 77.7^\circ)} \right| = 0.735$$

$$(VSWR)_{in} = \frac{1 + 0.735}{1 - 0.735} = 6.54$$