

MECHANICS OF COMPOSITE MATERIALS
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FORMULA SHEET FOR CHAPTER 3

$$\frac{E_2}{E_m} = \frac{1 + \xi \eta V_f}{1 - \eta V_f}, \eta = \frac{(E_f / E_m) - 1}{(E_f / E_m) + \xi}, \xi = 2$$

$$\frac{G_{12}}{G_m} = \frac{1 + \xi \eta V_f}{1 - \eta V_f}, \eta = \frac{(G_f / G_m) - 1}{(G_f / G_m) + \xi}, \xi = 1$$

$$(\sigma_1^c)_{ult} = \frac{E_1 (\varepsilon_2^T)_{ult}}{\nu_{12}} \quad \text{Matrix splitting}$$

$$(\varepsilon_2^T)_{ult} = (\varepsilon_m^T)_{ult} (I - V_f^{1/3})$$

$$(\varepsilon_2^T)_{ult} = (\varepsilon_m^T)_{ult} \left[\frac{d}{s} \left(\frac{E_m}{E_f} - 1 \right) + 1 \right]$$

$$(\sigma_1^c)_{ult} = \min \left[2 \left[V_f + (I - V_f) \frac{E_m}{E_f} \right] \sqrt{\frac{V_f E_m E_f}{3(I - V_f)}}, \frac{G_m}{I - V_f} \right]$$

$$(\sigma_1^c)_{ult} = 2 \left[(\tau_f)_{ult} V_f + (\tau_m)_{ult} V_m \right]$$

$$(\sigma_2^T)_{ult} = E_2 (\varepsilon_2^T)_{ult}$$

$$(\sigma_2^c)_{ult} = E_2 (\varepsilon_2^c)_{ult}$$

$$(\tau_{12})_{ult} = G_{12} \left[\frac{d}{s} \frac{G_m}{G_f} + \left(I - \frac{d}{s} \right) \right] (\gamma_m)_{ult}$$

$$\alpha_1 = \frac{1}{E_1} (\alpha_f E_f V_f + \alpha_m E_m V_m)$$

$$\alpha_2 = (I + \nu_f) \alpha_f V_f + (I + \nu_m) \alpha_m V_m - \alpha_1 \nu_{12}$$

$$\beta_1 = \frac{V_f E_f \Delta C_f \beta_f + V_m E_m \Delta C_m \beta_m}{E_1 (V_m \rho_m \Delta C_m + V_f \rho_f \Delta C_f)} \rho_c$$

$$\beta_2 = \frac{V_f (I + \nu_f) \Delta C_f \beta_f + V_m (I + \nu_m) \Delta C_m \beta_m}{(V_m \rho_m \Delta C_m + V_f \rho_f \Delta C_f)} \rho_c - \beta_1 \nu_{12}$$