

# Nonlinear Equations

Your nonlinearity confuses me

$$ax^5 + bx^4 + cx^3 + dx^2 + ex + f = 0$$

$$\tanh(x) = x$$

<http://nm.mathforcollege.com>

1

If for a real continuous function  $f(x)$ ,  $f(a)f(b) < 0$ , then in the domain  $[a, b]$  for  $f(x) = 0$ , there is (are)

0

one root

0%

undeterminable number of roots

0%

no roots

0%

at least one root

0%

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3

The velocity of a body is given by  $v(t) = 5e^{-t} + 4$ , where  $t$  is in seconds and  $v$  is in m/s. We want to find the time when the velocity of the body is 6 m/s. The equation form needed for bisection and Newton-Raphson methods is

0

$$f(t) = 5e^{-t} + 4 = 0$$

0%

$$f(t) = 5e^{-t} + 4 = 6$$

0%

$$f(t) = 5e^{-t} = 2$$

0%

$$f(t) = 5e^{-t} - 2 = 0$$

0%

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4

To find the root of an equation  $f(x) = 0$ , a student started using the bisection method with a valid bracket of  $[35, 55]$ . At the end of the 2nd iteration, the smallest range for the absolute true error for the root of the equation is

0

$$0 \leq |E_t| < 2.5$$

0%

$$0 \leq |E_t| < 5$$

0%

$$0 \leq |E_t| < 10$$

0%

$$0 \leq |E_t| < 20$$

0%

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5

Given an equation  $f(x) = 0$ , where  $f(x)$  is real and continuous, using the bisection method, one starts with a valid bracket of  $[x_l, x_u]$ . The first estimate of the root is then  $x_m = \frac{x_l + x_u}{2}$ . If now  $f(x_l)f(x_m) = 0$ ,

The new bracket is  $[x_m, x_u]$  0%

No new bracket is needed as  $x_l$  is the new root of the equation 0%

The new bracket is  $[x_l, x_m]$  0%

No new bracket is needed as  $x_m$  is the new root of the equation 0%

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6

Name one pitfall of the bisection method of solving nonlinear equations 0

Nobody has responded yet.  
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7

The formula for solving a nonlinear equation  $f(x) = 0$  by Newton Raphson Method is given by 0

$x_{i+1} = x_i - \frac{f'(x_i)}{f(x_i)}$  0%

$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)}$  0%

$x_{i+1} = x_i + \frac{f(x_i)}{f'(x_i)}$  0%

$x_{i+1} = x_i + \frac{f'(x_i)}{f(x_i)}$  0%

SEE MORE 0%

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8

Given  $f(x) = 7x^6 + 11x + 13$ , and if one wants to find a local minimum of the function, we would solve the equation in the following form for the Newton-Raphson method. 0

$7x^6 + 11x + 13 = 0$  0%

$42x^5 + 11 = 0$  0%

$210x^4 = 0$  0%

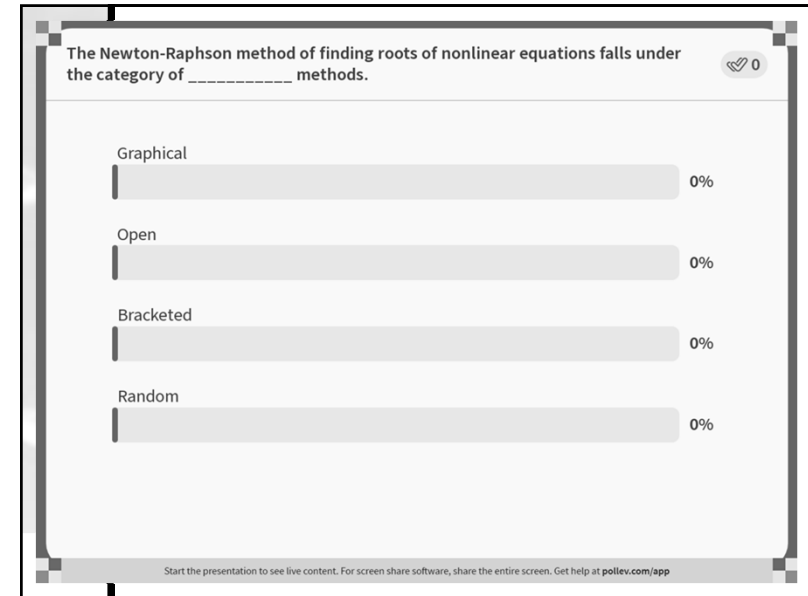
$7x^6 + 11x = -13$  0%

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11



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