

Ordinary Differential Equations

Everything is ordinary about them

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Physical Examples

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How long will it take to cool the trunnion?



$$mc \frac{d\theta}{dt} = -hA(\theta - \theta_a), \quad \theta(0) = \theta_{room}$$

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Classify the differential equation

$$3 \frac{dy}{dx} + 2y = e^x, \quad y(0) = 5$$

linear

0%

nonlinear

0%

linear with fixed constants

0%

indeterminable to be linear or nonlinear

0%

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Classify the differential equation

$$3x^3 \frac{dy}{dx} + 2x^2 y = e^x, y(0) = 5$$

linear 0%

nonlinear 0%

linear with fixed constants 0%

indeterminable to be linear or nonlinear 0%

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Classify the differential equation

$$3 \frac{dy}{dx} + 2y^2 = e^x, y(0) = 5$$

linear 0%

nonlinear 0%

linear with fixed constants 0%

indeterminable to be linear or nonlinear 0%

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Velocity of a body

The velocity of a body is given by $v(t) = e^{2t} + 5, t \geq 0$
Then the distance covered by the body from $t = 0$ to $t = 10$ can be calculated by solving the differential equation for $x(10)$ for

$\frac{dx}{dt} = e^{2t} + 5, x(0) = 0$ 0%

$\frac{dx}{dt} = e^{2t} + 5, x(0) = 5$ 0%

$\frac{dx}{dt} = 2e^{2t} + 5, x(0) = 0$ 0%

$\frac{dx}{dt} = \frac{e^{2t}}{2} + 5t, x(0) = 0$ 0%

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To solve $y' = f(x, y), y(0) = y_0$, the Euler's method formula is given by

$y = y + f(x, y)h$ 0%

$y_{i+1} = y_i + f(x_i, y_i)h$ 0%

$y_{i+1} = y_i + f'(x_i, y_i)h$ 0%

$y_{i+1} = f(x_i, y_i)h$ 0%

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The order of accuracy for a single step (local truncation error order) in Euler's method is

$O(h)$ 0%

$O(h^2)$ 0%

$O(h^3)$ 0%

$O(h^4)$ 0%

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The order of accuracy from initial point to final point (global truncation error order) while using more than one step in Euler's method is

$O(h)$ 0%

$O(h^2)$ 0%

$O(h^3)$ 0%

$O(h^4)$ 0%

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END

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