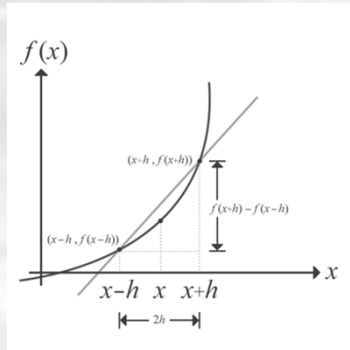


Differentiation

Audience Response Questions



<http://nm.mathforcollege.com>

1

Appropriate scheme

You are given the time-velocity data for a body

| | | | | | | |
|----------------|---|---|----|----|----|----|
| Time, t (s) | 0 | 1 | 6 | 8 | 11 | 15 |
| Velocity (m/s) | 1 | 8 | 15 | 18 | 22 | 29 |

Which one is the most appropriate scheme to use based on order of accuracy and data availability to calculate acceleration in $\frac{m}{s^2}$ at 8s?

Forward Divided
Difference Method

Central Divided
Difference Method

Backward Divided
Difference Method

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3

A possible formula for approximating the second derivative of a function $f(x)$ is

$$\frac{f(x+h) - f(x-h)}{2h}$$

$$\frac{f(x+h) - 2f(x) + f(x-h)}{h^2}$$

$$\frac{f(x+h) - 2f(x) + f(x-h)}{h}$$

$$\lim_{h \rightarrow 0} \frac{f(x+h) - 2f(x) + f(x-h)}{h^2}$$

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4

The order of accuracy of the central divided difference approximation

$$f'(x) \approx \frac{f(x+h) - f(x-h)}{2h}$$

Total Results: 0

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5

The highest order of polynomial for which the central divided difference gives the exact answer for its first derivative at any point is

Total Results: 0

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6

Velocity vs Time

The velocity vs time data is given below.

| | | | | | |
|-----------|---|-----|-----|-----|-----|
| t (s) | 0 | 0.5 | 1.2 | 1.5 | 1.8 |
| v (m/s) | 0 | 213 | 223 | 275 | 300 |

The data points at $t=1.2$, 1.5 and 1.8 are interpolated to a 2nd order polynomial to give $v(t) = -150t^2 + 578.33t - 255, 1.2 \leq t \leq 1.8$
The best estimate of acceleration at $t=1.5$ in m/s^2 using the polynomial is

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7

Using central divided difference, the true error in the calculation of a derivative of a function is 32.0 for a step size of 0.4. If the step size is reduced to 0.1, the true error will be approximately

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