

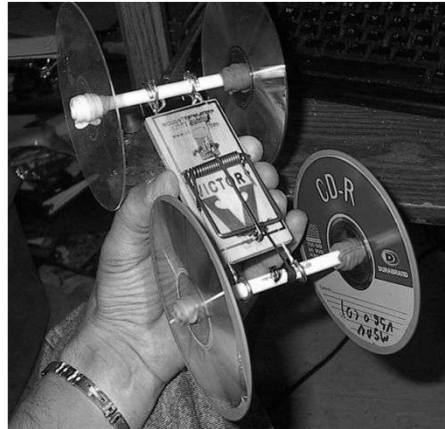
Regression

<http://nm.mathforcollege.com>

Applications

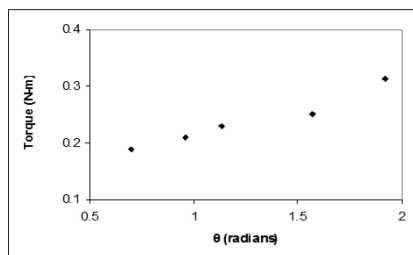
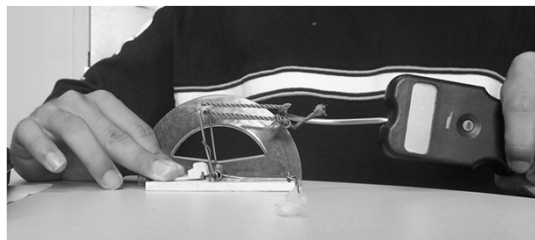
<http://nm.mathforcollege.com>

Mousetrap Car



<http://nm.mathforcollege.com>

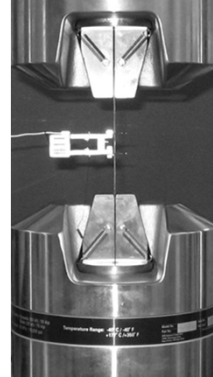
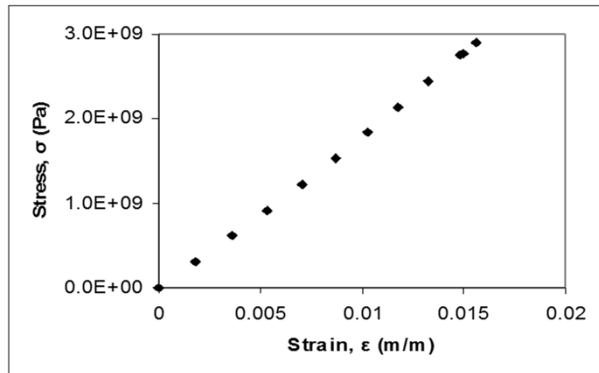
Torsional Stiffness of a Mousetrap Spring



$$T = k_0 + k_1 \theta$$

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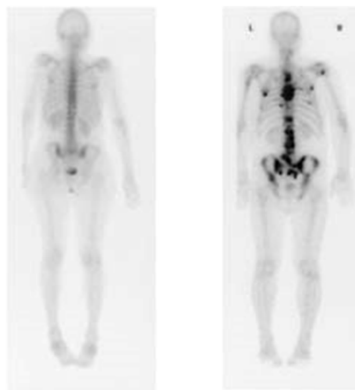
Stress vs Strain in a Composite Material



$$\sigma = E\epsilon$$

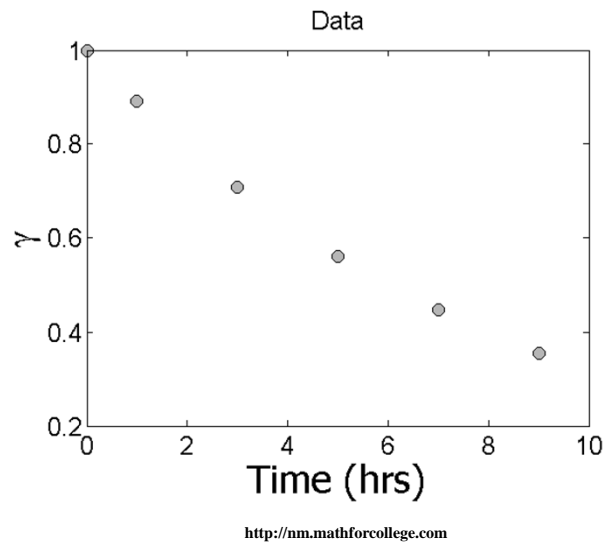
<http://nm.mathforcollege.com>

A Bone Scan

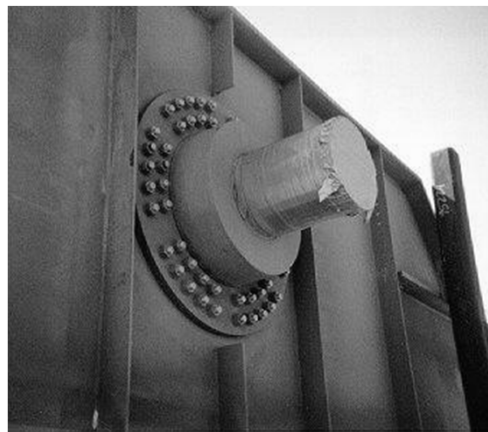


<http://nm.mathforcollege.com>

Radiation intensity from Technetium-99m

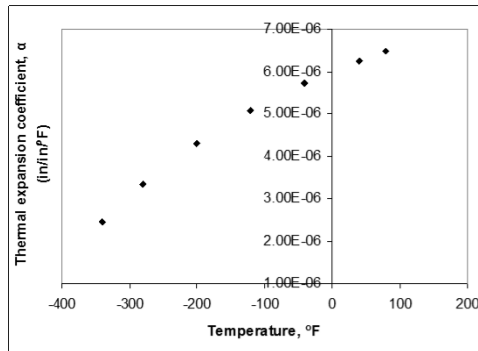


Trunnion-Hub Assembly



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Thermal Expansion Coefficient Changes with Temperature?



$$\alpha = a_0 + a_1T + a_2T^2$$

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THE END

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Pre-Requisite Knowledge

<http://nm.mathforcollege.com>

This rapper's name is

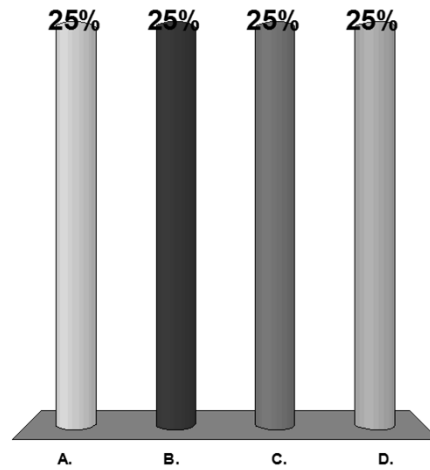
- A. Da Brat
- B. Shawntae Harris
- C. Ke\$ha
- D. Ashley Tisdale
- E. Rebecca Black



<http://nm.mathforcollege.com>

Close to half of the scores in a test given to a class are above the

- A. average score
- B. median score
- C. standard deviation
- D. mean score

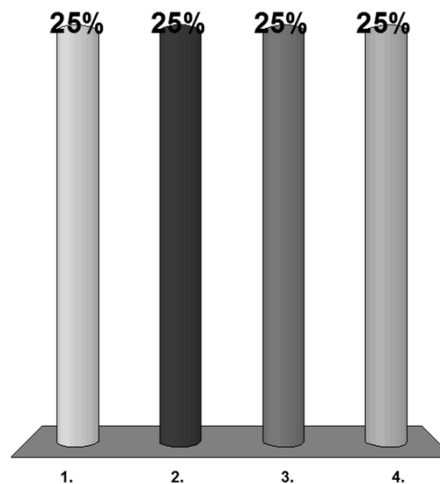


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The average of the following numbers is

2	4	10	14
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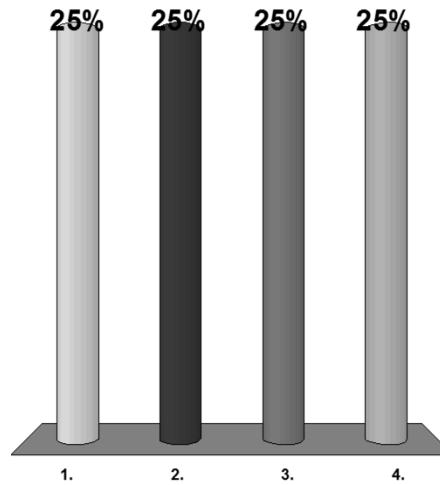
- 1. 4.0
- 2. 7.0
- 3. 7.5
- 4. 10.0



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The average of 7 numbers is given 12.6. If 6 of the numbers are 5, 7, 9, 12, 17 and 10, the remaining number is

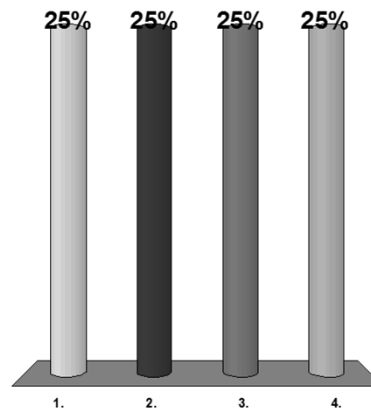
1. -47.9
2. -47.4
3. 15.6
4. 28.2



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Given y_1, y_2, \dots, y_n , the standard deviation is defined as

- A. $\cdot \sum_{i=1}^n [y_i - \bar{y}]^2 / n$
- B. $\cdot \sqrt{\sum_{i=1}^n [y_i - \bar{y}]^2 / n}$
- C. $\cdot \sum_{i=1}^n [y_i - \bar{y}]^2 / (n-1)$
- D. $\cdot \sqrt{\sum_{i=1}^n [y_i - \bar{y}]^2 / (n-1)}$



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THE END

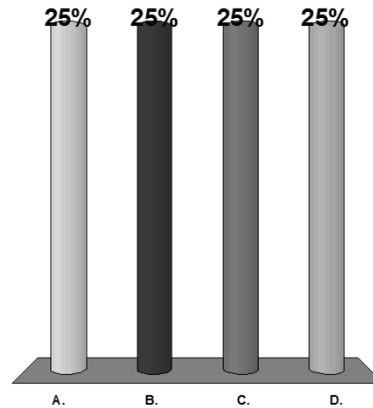
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6.03
Linear Regression

<http://nm.mathforcollege.com>

Given $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$, best fitting data to $y=f(x)$ by least squares requires minimization of

- A. $\sum_{i=1}^n [y_i - f(x_i)]$
- B. $\sum_{i=1}^n |y_i - f(x_i)|$
- C. $\sum_{i=1}^n [y_i - f(x_i)]^2$
- D. $\sum_{i=1}^n [y_i - \bar{y}]^2, \bar{y} = \frac{\sum_{i=1}^n y_i}{n}$



<http://nm.mathforcollege.com>

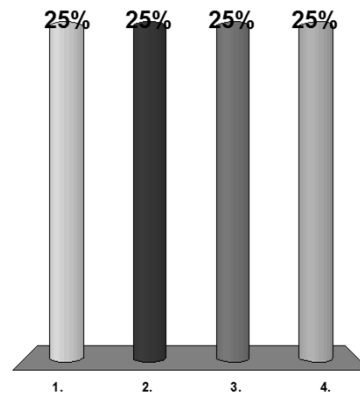
The following data

x	1	20	30	40
y	1	400	800	1300

is regressed with least squares regression to $y=a_1x$.

The value of a_1 most nearly is

- A. 27.480
- B. 28.956
- C. 32.625
- D. 40.000



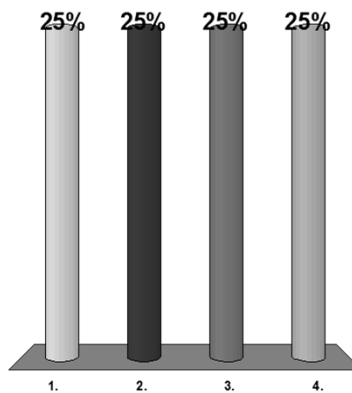
<http://nm.mathforcollege.com>

A scientist finds that regressing y vs x data given below to straight-line $y=a_0+a_1x$ results in the coefficient of determination, r^2 for the straight-line model to be **zero**.

x	1	3	11	17
y	2	6	22	?

The missing value for y at $x=17$ most nearly is

- A. -2.444
- B. 2.000
- C. 6.889
- D. 34.00



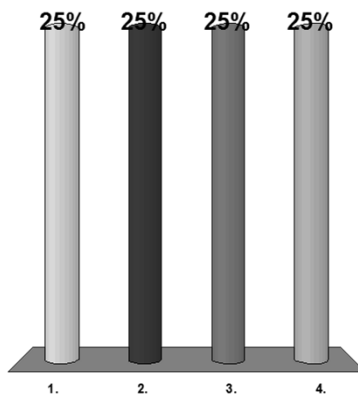
<http://nm.mathforcollege.com>

A scientist finds that regressing y vs x data given below to straight-line $y=a_0+a_1x$ results in the coefficient of determination, r^2 for the straight-line model to be **one**.

x	1	3	11	17
y	2	6	22	?

The missing value for y at $x=17$ most nearly is

- A. -2.444
- B. 2.000
- C. 6.889
- D. 34.00



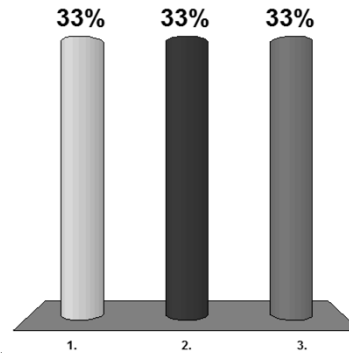
<http://nm.mathforcollege.com>

The following data

x	1	20	30	40
y	1	400	800	1300

is regressed with least squares regression to a straight line to give $y = -116 + 32.6x$. The **observed** value of y at $x=20$ is

- A. -136
- B. 400
- C. 536



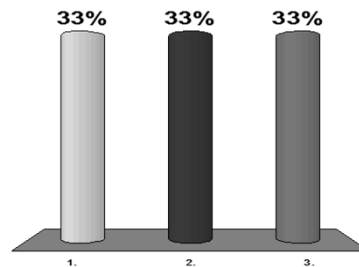
<http://nm.mathforcollege.com>

The following data

x	1	20	30	40
y	1	400	800	1300

is regressed with least squares regression to a straight line to give $y = -116 + 32.6x$. The **predicted** value of y at $x=20$ is

- A. -136
- B. 400
- C. 536



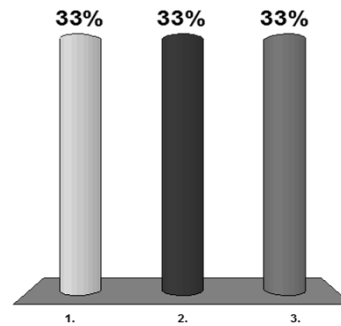
<http://nm.mathforcollege.com>

The following data

x	1	20	30	40
y	1	400	800	1300

is regressed with least squares regression to a straight line to give $y = -116 + 32.6x$. The **residual** of y at $x=20$ is

1. -136
2. 400
3. 536



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THE END

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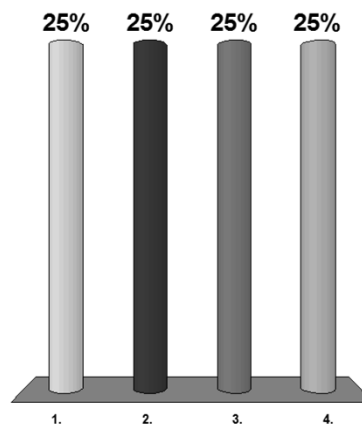
6.04

Nonlinear Regression

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When transforming the data to find the constants of the regression model $y = ae^{bx}$ to best fit $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$, the sum of the square of the residuals that is minimized is

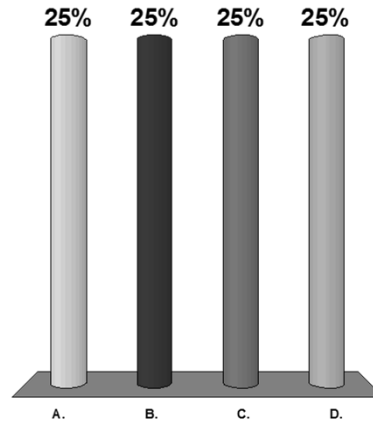
- A. $\sum_{i=1}^n (y_i - ae^{bx_i})^2$
 B. $\sum_{i=1}^n (\ln(y_i) - \ln a - bx_i)^2$
 C. $\sum_{i=1}^n (\ln(y_i) - \ln a - b \ln(x_i))^2$
 D. $\sum_{i=1}^n (y_i - \ln a - bx_i)^2$



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When transforming the data for stress-strain curve $\sigma = k_1 \varepsilon e^{-k_2 \varepsilon}$ for concrete in compression, where σ is the stress and ε is the strain, the model is rewritten as

- A. $\ln \sigma = \ln k_1 + \ln \varepsilon - k_2 \varepsilon$
- B. $\ln \frac{\sigma}{\varepsilon} = \ln k_1 - k_2 \varepsilon$
- C. $\ln \frac{\sigma}{\varepsilon} = \ln k_1 + k_2 \varepsilon$
- D. $\ln \sigma = \ln(k_1 \varepsilon) - k_2 \varepsilon$



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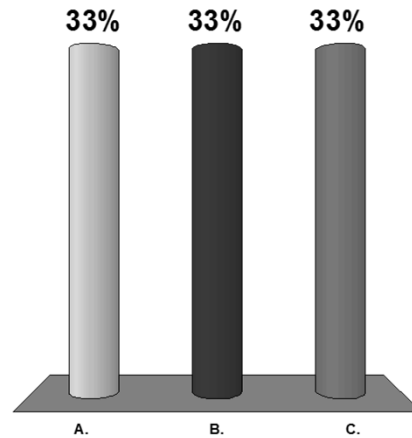
6.05

Adequacy of Linear Regression Models

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The case where the coefficient of determination for regression of n data pairs to a straight line is **one** if

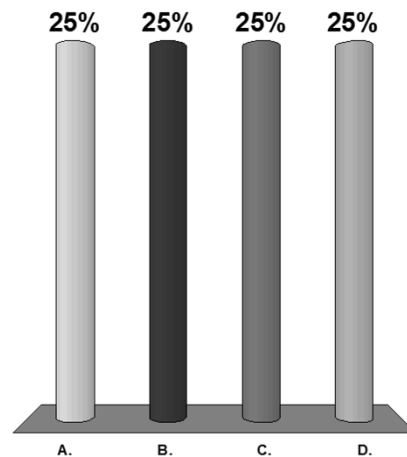
- A. none of data points fall exactly on the straight line
- B. the slope of the straight line is zero
- C. all the data points fall on the straight line



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The case where the coefficient of determination for regression of n data pairs to a general straight line is **zero** if the straight line model

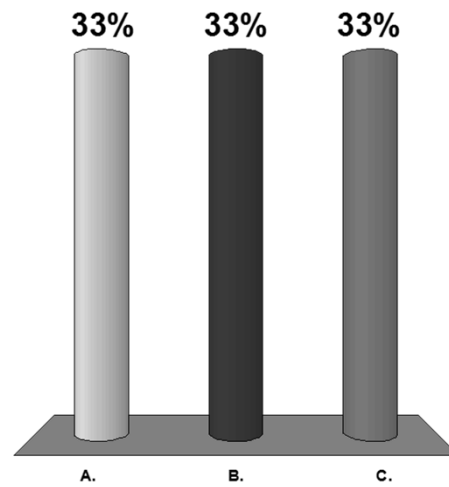
- A. has zero intercept
- B. has zero slope
- C. has negative slope
- D. has equal value for intercept and the slope



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The coefficient of determination varies between

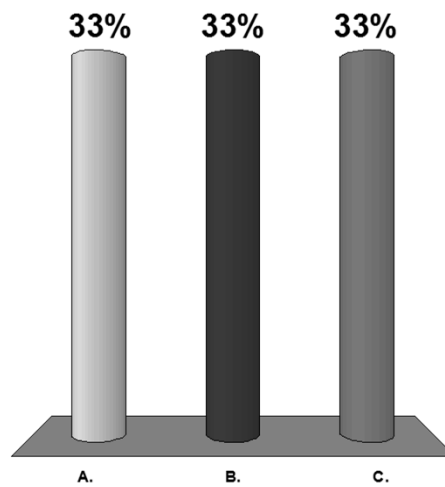
- A. -1 and 1
- B. 0 and 1
- C. -2 and 2



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The correlation coefficient varies between

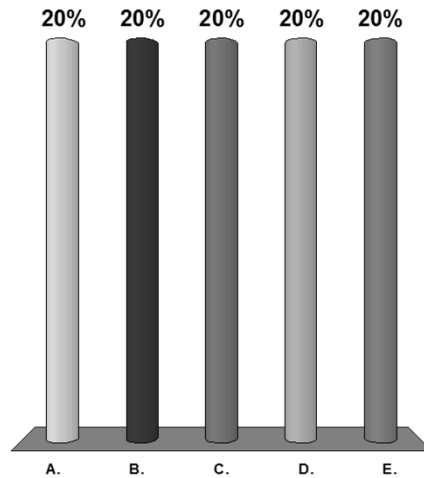
- A. -1 and 1
- B. 0 and 1
- C. -2 and 2



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If the coefficient of determination is 0.25, and the straight line regression model is $y=2-0.81x$, the correlation coefficient is

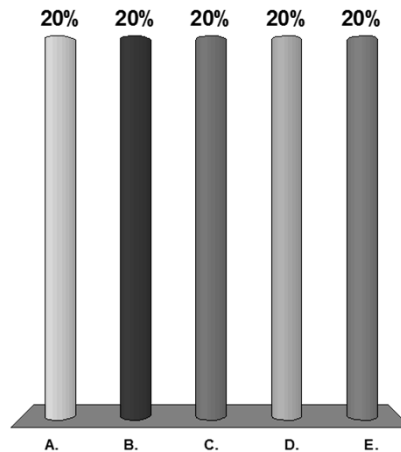
- A. -0.25
- B. -0.50
- C. 0.00
- D. 0.25
- E. 0.50



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If the coefficient of determination is 0.25, and the straight line regression model is $y=2-0.81x$, the strength of the correlation is

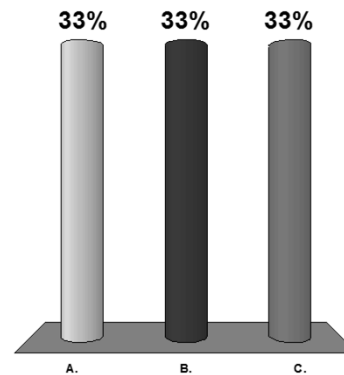
- A. Very strong
- B. Strong
- C. Moderate
- D. Weak
- E. Very Weak



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If the coefficient of determination for a regression line is 0.81, then the percentage amount of the original uncertainty in the data explained by the regression model is

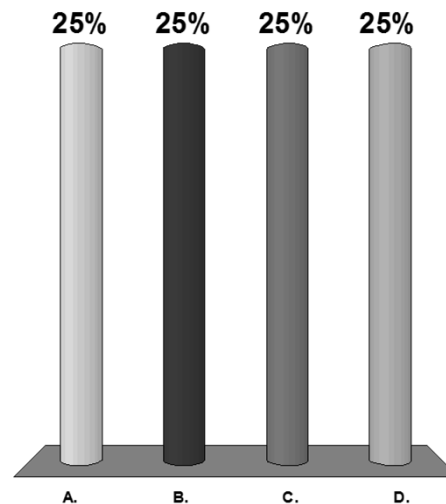
- A. 9
- B. 19
- C. 81



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The percentage of scaled residuals expected to be in the domain $[-2, 2]$ for an adequate regression model is

- A. 85
- B. 90
- C. 95
- D. 100



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