Potential-Dependent Chloride Threshold in Reinforced Concrete Damage Prediction – Effect of Activation Zone Size

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ABSTRACT

Previous work has shown that chloride corrosion threshold increases when steel bar potentials are more cathodic than -200±50 mV (SCE). When corrosion starts at a given location, the steel of the adjacent regions remains in its passive state; therefore corrosion initiation is delayed in those regions due to the negative shift in potential. Introduction of threshold dependence on potential is a critical need for accurate forecasting, as neglecting that phenomenon can lead to erroneously high damage projections. An earlier investigation incorporated this issue in a one-dimensional deterministic model solved by a finite difference method evaluating a partially submerged reinforced concrete column. While the model served to demonstrate feasibility of the concept, damage prediction was found to be highly sensitive to the corrosion activation zone size. As the number of nodes used for the model increased, resulting in smaller activation zones, the total predicted amount of damage at a given age decreased. Examination of the model assumptions suggested that the problem stemmed from neglecting the local resistance of the concrete around the steel bars. An improvement has been developed here by implementing a formulation that accounts for the local resistance polarization associated with the selection of the size of activation zone. The damage projections for the smaller node separation resulted in a finite limiting value. Comparison with a case where the effect of local resistance polarization in the activation zone size is neglected is presented.

Key words: chloride corrosion threshold, modeling, steel potential, corrosion, concrete, active zone size, resistance polarization.

INTRODUCTION

Corrosion of steel in concrete initiates once the concentration of chloride ions at the steel surface reaches a minimum required amount, defined as the chloride corrosion threshold, C_T. Corrosion forecasting models largely follow Tuutti’s initiation-propagation stages concept.1 There the

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value of $C_T$ plays a key role in commonly used approaches to estimate the length of the initiation stage, along with the chloride surface concentration ($C_S$), chloride diffusion coefficient ($D$), and concrete cover ($X_C$). While the value of $C_T$ is assigned a random range of variability in some model implementations, $C_T$ is commonly assumed to be time invariant and not affected by the corrosion state of nearby portions of the rebar assembly.\(^2\)

There is increasing evidence that the chloride corrosion threshold increases when the still passive steel is polarized to potential values more cathodic than the typical open circuit potential in atmospherically exposed concrete. The latter is in the order of $\sim -100 \text{ mV}$ versus saturated calomel electrode (SCE; all potentials in the following will be reported in this scale).\(^3\) An updated version of a literature review by Presuel et al on the relationship between $C_T$ and steel potential ($E$) is shown in Figure 1.\(^2,4\) Despite the scatter, it can be seen that at potentials $\sim -100 \text{ mV}$ the values of $C_T$ are roughly independent of $E$, but that at more negative potentials the values of $C_T$ tend to follow an exponential increase with additional cathodic polarization. A recent investigation by Sánchez and Sagüés [2] (gray diamonds in Figure 1) provided further support of that threshold dependence on potential (TDP) trend. An envelope trend line, such as that drawn in Figure 1, may be described in general terms by Equation (1):

$$\log_{10}\left(\frac{C_T}{C_{T0}}\right) \sim \frac{E_{T0} - E}{\beta_{CT}}$$  

where $C_T$ is the threshold expressed as percentage of cement content in the concrete, $E$ is the potential of the steel bar, while still in the passive condition, $\beta_{CT}$ is the characteristic inverse slope of the increase of $C_T$ in a $E$-$\log C_T$ representation and $E_{T0}$ and $C_{T0}$ are constants. This effect is the basis of the cathodic prevention method, whereby reinforcing steel is cathodically polarized while still in the passive condition to delay or prevent corrosion due to the elevation of the corrosion threshold.\(^5,6\)

![Figure 1. Chloride threshold dependence on steel potential compilation by Presuel, updated by Sánchez.\(^4,2\)](chart.png)

**Notation:** OPC: Ordinary Portland Cement; SRC: Sulfate resistant cement; BFSC: Blast furnace slag cement; M: mortar or C: concrete; P: Polarized or F: open circuit potential; I: Immersed or N: Not Immersed; X: cyclic or permanent ponding; Y: splash zone or Z: simulated splash zone. Dashed line: see text.
The redundant 3-parameter line formulation is chosen for convenience to match the form of other ruling equations in electrochemical systems.\textsuperscript{7} The dashed trend line shown in Figure 1 corresponds to values of $E_{T0} = -0.128$ V, $C_{T0} = 0.2$ % and $\beta_{CT} = -0.4$ V. Those parameter values, which represent a conservative lower envelope of the data\textsuperscript{(1)} had been used in preceding TDP modeling simulations and were adopted for consistency in the present work as well. That choice is however not limiting and other parameter selections, presented elsewhere, may be more representative for engineering forecasting purposes.\textsuperscript{2,6-10}

Introduction of TDP is important for accurate corrosion forecasting, as neglecting that phenomenon can lead to erroneously high damage projections. This was shown in the previous work that incorporated TDP in a finite difference deterministic model of a partially submerged reinforced concrete column.\textsuperscript{8} The column was divided into zones of equal size. A surface chloride concentration pattern was assumed, as well as diffusional transport of chlorides into the concrete. Initially the steel potential was nearly uniform corresponding to a passive steel condition, which resulted in a threshold value that was nearly the same everywhere.

Corrosion started when the chloride corrosion threshold was first reached at the zone having the highest surface chloride content. That event resulted in activation of that zone and the creation of a macrocell corrosion pattern where that zone was anodic while the rest of the steel in the column remained as a passive, cathodic zone. The corrosion macrocell pattern for that configuration was then calculated to obtain the value of the steel potential $E$ at every zone in the system. The still passive zones near that first activated developed a significantly more negative value of $E$ than the one present before the first activation event. Hence, those zones where assigned per Eq. (1) a correspondingly larger value of $C_T$ than before. Corrosion initiation in those regions was consequently delayed. As the newly calculated threshold value was eventually reached in other zones, the macrocell pattern was affected accordingly and corrosion development delayed in nearby regions as well. The overall result is a slower progression of corrosion in the system than if the threshold would have been a constant, potential-independent value. The effect, illustrated in Figure 2, was found to be a dramatic decrease in the predicted amount of corrosion damage when $\beta_{CT}$ was finite (TDP) compared to the case of a potential-independent threshold ($\beta_{CT} = \infty$).

While those initial calculations served to reveal the importance of introducing TDP, that early model implementation had shortcomings that needed further resolution. In particular, it was noted that damage prediction was highly sensitive to the corrosion activation zone size.\textsuperscript{8} It was found that as the number of nodes used for the model increased, resulting in smaller activation zones, the total projected amount of damage at a given age decreased toward a zero limit value when node spacing was zero. That trend was clearly erroneous and constituted a major limitation in including TDP in damage projections.

Examination of the model assumptions suggested that the problem stemmed from neglecting the local resistance of the concrete around the steel bars. As a result, the macrocell coupling effect was inappropriately exaggerated as node spacing decreased leading to an erroneous limit condition. This paper presents a successful resolution of that issue by implementing an improved formulation that accounts for the local resistance polarization consistent with the size of activation zone.

\textsuperscript{(1)} For example with a concrete with cement factor $C_F = 355$ Kg/m$^3$ (600 pcy) the resulting value of $C_T$ at $E_{T0}$, near typical open circuit potentials, is 0.71 Kg/m$^3$ (1.2 pcy), which is an often adopted conservative threshold value.
Damage projections in previous model calculations showing strong decrease in projected damage at age=60 years when comparing the case of a potential independent threshold ($\beta_{CT} = \infty$) and cases where $C_T$ depended on potential of the passive steel. [8].

**SYSTEM DETAILS**

An illustration of the system modeled in the improved formulation is shown in Figure 3. It consists of a cylindrical reinforced concrete structure exposed to a marine environment and submerged to half its length $L$. It has a diameter $\phi$, concrete cover $X_C$ where the rebar mat is located. The following system description is identical to the one discussed in Reference 9.

The system chosen for representation is a marine substructure, solid cylindrical reinforced concrete column partly submerged in seawater, of dimensions equivalent to those used when first introducing the potential-dependent threshold model. For simplicity, an idealized one-dimensional model was used here to represent the column, comparable to that employed by the authors in related work. As shown there, that approach captures most of the features of interest of the system with minimum computational burden. The rebar mat, treated as a uniform sheet, has a total surface area of steel exposed to concrete equal to the external lateral column surface area multiplied by a Steel Factor $S_F$. The ends of the cylindrical column are considered to be isolated electrically and from the surrounding environment, and with no reinforcement.

The column is assumed to be immersed in seawater to half its length. The concrete is approximated as an effectively homogeneous electrolytic medium of resistivity $\rho$, effective chloride ion diffusivity $D$, and effective oxygen diffusivity $D_O$ all of which are functions of elevation. Concrete on the lateral surface of the column is assumed to have developed very early a time-invariant chloride ion concentration $C_S$ that is a function of elevation, and a time-invariant effective oxygen concentration $C_{SO}$ treated as being constant with elevation.
Figure 3. System modeled. Cases evaluated in this work. Dashed lines discuss cases examined.

The reinforcing steel is assumed to be the locus of an anodic metal loss reaction as shown in Equation (3)

$$Fe \rightarrow Fe^{+2} + 2e^-$$

with a corresponding current density $i_a$, under two modalities: passive dissolution at a fixed small current density $i_p$, or active dissolution at a potential-dependent current density $i_{aa}$ so that Equation (3a)

$$i_a = i_p \quad \text{(passive state)}$$

And Equation (3b):

$$i_a = i_{aa} = i_{oa} 10^{\left(\frac{E-E_{oa}}{\beta_a}\right)} \quad \text{(active state)}$$

where $i_{oa}$ is the nominal exchange current density, $E_{oa}$ is the nominal equilibrium potential and $\beta_a$ is the anodic Tafel slope. The steel is also assumed to support a single cathodic reaction, oxygen reduction, Equation (4):

$$O_2 + 2H_2O + 4e^- \rightarrow 4OH^-$$
which is considered for simplicity to occur under either a fully activation-controlled or a fully diffusion-
limited conditions. Under full activation control the current density is

\[ i_{ca} = i_c = i_{oc} 10^{\frac{(E_{oc} - E)}{\beta c}} \]  

(5)

where \( i_{oc} \) is the nominal exchange current density, \( E_{oc} \) is the nominal equilibrium potential and \( \beta c \) is the cathodic Tafel slope. Under full diffusional control the current density is Equation (6):

\[ i_{cd} = i_c = \frac{4FDc_{SO}D_0}{k_cS_F} \]  

(6)

where 4 is the number of electrons to reduce \( O_2 \), \( F = 96.5 \ 10^3 \) coul/equiv is Faraday's constant, \( c_{SO} \) is the oxygen concentration in the pore water at the external concrete surface, and \( DO \) is the effective diffusion coefficient of \( O_2 \) in the concrete, scaled to match the concentration units used. The value of \( i_c \) is made to switch from \( i_{ca} \) to \( i_{cd} \) when the former exceeds the latter, creating a working approximation in lieu of the more computationally mixed polarization function.\(^{12}\)

As indicated in previous papers, the model computes the accumulation of chloride at the steel surface with time and declares elements active as the local value of \( C_T \) is exceeded.\(^{8,9}\) The corrosion propagation stage is addressed by computing the increasing amount of steel loss and declaring a given segment as damaged when a critical corrosion penetration amount is exceeded. Those features of the model are addressed in detail in the previous publications and will not be further treated here. In more detail the following concerns the computation of corrosion current distribution and potentials in the system, which is relevant to the new features introduced here.

Calling \( x \) the distance along the column axis, defining and treating the problem as one-dimensional in a manner similar to that used in Reference\(^{11}\) the charge conservation condition implies that Equation (7):

\[ i_s = \left( \frac{\frac{\rho}{4S_F}}{\frac{1}{\rho} \frac{d^2E}{dx^2} + \frac{dE}{dx}} \right) \]  

(7)

where \( i_s = i_a - i_c \) is the net current density on the steel surface at elevation \( x \), with \( i_s \) being equal to \( i_{wa} \) or \( i_p \) depending on whether the local steel surface was declared active or passive respectively if the value of \( C \) was respectively above or below the value of \( C_T \).

Solution of Eq. (7) to obtain \( i_s \) and \( E \) as function of \( x \) is conducted iteratively for each time \( t \) using finite differences on a 101-node equispaced array along the elevation direction. The declaration of whether a given node corresponds to active or passive steel is made using the value of chloride concentration predicted by solution of Fick’s 2\(^{nd}\) law (as indicated in the previous papers [8,9]), and the local value of \( C_T \) calculated at each node per Eq.(1) using the value of \( E \) obtained at the end of the iterations conducted in the previous time step. The array of values of \( C_T \) remains unchanged during the iteration process. After iteration is complete the potential array is used as seed for the next time step potential calculations. It is noted that once steel at a given node is declared active, it remains so for all subsequent time steps. This is only a simplifying assumption that may be refined in future implementations of the modeling concept.

Equation (7) results from considering that the net current of the steel present in a length \( dx \) of column is equal to the difference in longitudinal current at each end of the element, as in a transmission line calculation. The respective current densities are inversely proportional to the lateral active surface of the element \( S_F \pi \Phi dx \), and the cross sectional area of the element \( S_F \pi \Phi^2/4 \); the factors combine as shown when expressed in differential form. The longitudinal current density is proportional to the local longitudinal electric field. The formulation can be expressed equivalently in discretized electric circuit form as shown in Figure 4 following the treatment by Presuel, with segmental longitudinal resistance \( R_L \)
(Equation 8) and interfacial terms $E_{Si}$ related to $i_{si}$ by the polarization equations given above and illustrated in Figure 5.\textsuperscript{11}

Figure 4. System discretization and types resistances used in the system showing a portion of the column near the waterline, starting at node $i$. Black resistor: longitudinal resistance. Dashed resistor: radial resistance. Gray resistor: steel resistance.

\[
R_L = \frac{\Delta X \rho}{(\pi \phi^2)}
\]  

Figure 5. Longitudinal resistance for a segment $\Delta X$
where ΔX is the distance along the column axis, ρ is the local value of the concrete resistivity, φ is the diameter of the column.

In the simplified treatments given in previous versions of the model in References\textsuperscript{8,10} for the above-water nodes was the same as the potential in the concrete in the same node, effectively assuming that there was no substantial potential drop between the rebar surface and the concrete nearby. Thus, any local resistance associated with geometric current constriction around the steel was considered negligible so the current density on the rebar surface was subject only to activation and concentration polarization (of the cathodic reaction only) of the reactions involved. For anodic segments providing cathodic prevention to surrounding passive regions, the activation-only limited anodic reaction was dominant, and it was unencumbered by the presence of a resistive term. Given the kinetic parameter choices used i, the resulting prevention effect extended over a relatively large region even if the active zone associated with a node was very small. In the below water segments a radial resistance factor was included called R\textsubscript{r}, but only as a global factor that again did not sufficiently capture any local current concentration effect. That shortage was addressed here; by introducing a local resistance term R\textsubscript{S} that was evaluated as follows.

The rebar was treated as a narrow cylindrical electrode of radius \(\phi_r/2\) in a cylindrical medium that extended to an influence radius \(r_{iz}\) that is roughly approximated as \(\frac{1}{2}\) of \(\phi\) (Figure 6) as shown in Equation (9):

\[
 r_{iz} = \frac{1}{2} \phi \tag{9}
\]

Using the equation for the resistance between concentric cylinders\textsuperscript{13}, the current concentration resistance per unit length of rebar \(R_{SUL}\) is given by Equation (10):

\[
 R_{SUL} = \frac{\rho}{2\pi} \ln \left( \frac{r_{iz}}{\phi_r} \right) \tag{10}
\]

Accounting for the length of rebar associated with \(S_F\) and the column dimensions, the amount of resistance \(R_S\) for each segment due to current concentration around the rebar is given by Equation (11)

\[
 R_S = \frac{R_{UL} \phi_r}{S_F \phi \Delta X} \tag{11}
\]

**Figure 6. Local steel resistance (R\textsubscript{S}) for a segment ΔX.**

Introduction of Rs requires accounting for the potential difference between the immediate steel surface and the bulk of the surrounding concrete. In the previous model in Reference\textsuperscript{8} the term E described indistinctly the potential next to the steel surface and that in the bulk of the concrete. In the present treatment those are named \(E_S\) and \(E_c\) respectively and related to each other as shown in Eq.(12) and Fig.7 due to the presence of local resistance. \(E_S\), the steel potential with respect to an ideal reference
electrode placed immediately next to the steel, rules the rate of the electrochemical reactions and hence needs to be used instead of \( E \) in Eqs. 3b and 5.

\[
E_s = E - i_s R_s
\]  
(12)

**Figure 7. Relationship between \( E_c \) and \( E_s \)**

Likewise, \( E_c \) rules the ohmic interaction between column segments and needs to be used instead of \( E \) in Eq. (8). The computation scheme was adjusted accordingly by making the necessary link between both potentials through Eq. 16. Introduction of \( R_s \) in the model captured a key element in providing a more realistic representation of the system, and in allowing simulations to converge toward a stable limit as the segment size was decreased. As implied by Eq. (14), a decreased segment size (equivalent to decreasing the size of the activation zone) increases the value of \( R_s \) and hence the relative extent of resistance polarization of the segment reactions.

**ACTIVE ZONE SIZE**

The expected relationship between activation zone and corresponding throwing power of the cathodic prevention effect can be further illustrated by the idealization shown in Figure 8. Here a portion of an individual rebar is addressed for clarity instead of the rebar in an entire column segment, but the overall concept applies in both cases.

A steel bar (initially in the passive state) is embedded in concrete with fixed \( C_T \) and \( E_s \) is represented in Figure 8 (a). Figure 8 (b and c) shows that after some time chloride ions coming non-uniformly from the exterior (1) caused \( C_T \) to be exceeded in a small zone where the passive film on the steel breaks down. A corrosion macrocell is formed with drop of \( E_s \) towards more negative values (3) around the active zone. The steel surrounding the active zone is still protected by the passive film, but due to macrocell coupling \( E \) in these regions (4) has a significantly lower value compared to the rest of the passive steel. Therefore \( C_T \) increases in these regions (per Eq. (1)) delaying corrosion initiation there. Figure 8 (c) illustrates a similar situation, but there the size of the activation zone was larger than that in 8b, and the size of the surrounding region where the increase in \( C_T \) is substantial is correspondingly larger as well. The influence zone is smaller with smaller activation zones because the macrocell effect is ohmically limited by local current constriction around a small anode. As activation zones become smaller, the corrosion preventing effect becomes smaller as well, and while the amount of corrosion per event is smaller, the number of events is expected to increase so a limiting condition is anticipated where the lower degree of corrosion mitigation is matched by the larger number of corroding spots.
Figure 8. Passive and active state of a steel bar embedded in concrete considering the size of the activation spot. a) System at a passive state, b) system at an active state with small active spot, c) system at an active state with large active spot.

CASES EXAMINED

Base Case-NR corresponds to the input parameters evaluated in the so called “base case” in the previous model calculations [8] addressing resistance $R_L$ only. Base Case-R is similar to Base Case-NR but incorporates the resistance $R_S$ introduced here to address the activation zone size dependence noted above. Two other cases, Low DO$_2$ and $\rho$-NR and Low DO$_2$ and $\rho$-R are as in each of the above cases respectively, but in each the system has lower concrete resistivity and lower oxygen diffusivity. A summary of the model parameters are given in Table 1. The threshold dependence on potential in all these cases is assumed to correspond to a value of $\beta_{CT} = 0.4$ V.

As explained in a previous Reference$^8$ lower resistivity and lower oxygen diffusivity are both expected to lead to a greater corrosion macrocell influence zone. Hence in these cases the effect of introducing TDP is expected to be stronger. These added cases offer a wider range of conditions in
which to evaluate to which extent introduction of $R_S$ in the calculations acts to stabilize the limit response to activation zone decrease.

All cases were simulated by conducting calculations that included active zones equal to $\frac{1}{2}$, $\frac{1}{4}$ and $\frac{1}{8}$ times less than the steel element surface area of the “Base Case” from the previous model implementation in References$^8$ which was done with a 101 node array. Those calculations were therefore made with numbers of nodes ranging from 101 to 801.

Table 1. Model parameters

<table>
<thead>
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<th>MODEL PARAMETERS</th>
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<tr>
<td>Steel Cover</td>
<td>$X_c = 10.5$ cm</td>
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<tr>
<td>Column diameter</td>
<td>$D = 105$ cm</td>
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<tr>
<td>Column Length</td>
<td>$L = 1200$ cm</td>
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<tr>
<td>Cement factor</td>
<td>$C_F = 355$ Kg/m$^3$</td>
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<td>Concrete Resistivity (Base Case)</td>
<td>$\rho_H = 2 \times 10^5$ ohm-cm</td>
</tr>
<tr>
<td></td>
<td>$\rho_L = 4 \times 10^4$ ohm-cm</td>
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<tr>
<td>Concrete Resistivity (Low)</td>
<td>$\rho_H = 4 \times 10^4$ ohm-cm</td>
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<td></td>
<td>$\rho_L = 4 \times 10^4$ ohm-cm</td>
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<tr>
<td>Oxygen Diffusivity (Base Case)</td>
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<td>$D_{OL} = 10^{-5}$ cm$^2$/sec</td>
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<tr>
<td>Oxygen Diffusivity (Low)</td>
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<td></td>
<td>$D_{OL} = 10^{-5}$ cm$^2$/sec</td>
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<tr>
<td>Chloride Diffusivity</td>
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<td>$O_2$ Surface Concentration</td>
<td>$C_{SO} = 2.5 \times 10^{-7}$ mol/cm$^3$</td>
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<td>Cl Surface Concentration</td>
<td>$C_{SN} = 15$ Kg/m$^3$</td>
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<td>$C_{SW} = 9$ Kg/m$^3$</td>
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<td></td>
<td>$C_{SL} = 0$ Kg/m$^3$</td>
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<td>Chloride Threshold Parameters</td>
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<td>$E_T$ (-128 mV)</td>
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<td>$i_p = 6.25 \times 10^{-10}$ A/cm$^2$</td>
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<td>Critical Corrosion Penetration</td>
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<td></td>
<td>Corresponding to $\frac{1}{2}$, $\frac{1}{4}$ and $\frac{1}{8}$ base case node</td>
</tr>
</tbody>
</table>

RESULTS AND DISCUSSION

Figure 9 compares the damage projection values, expressed as percentage of the column surface affected by corrosion spalls, for 60 years of service life for calculations that incorporate the effect of $R_S$ (open symbols), and those not incorporating it as the previous modeling approach (solid symbols)$^8$. The results are given as function of the active zone size, expressed as fraction of the size corresponding to the 101 node array simulation. As shown there, the projected amount of damage decreases, nearly linearly, with decreasing activation zone size. The red dashed lines represent a linear approximation of the resulted data points for all the cases, extrapolated to activation zone size equals zero. It is noted that the Base Case-NR calculations for the 101 node array simulation (fraction =1 in the horizontal axis) is the same case for which the results were depicted for $\beta$=0.4 V in Figure 2.

When local resistance was not taken into account (NR cases), the decrease of the damage projection with activation zone size was, for both variations of resistivity and oxygen diffusivity, toward nearly zero values for a terminally small node separation. The linear trend fit indicated ~0.4 % and -0.04% for the Base Case-NR and the Low DO$_2$ and $\rho$-NR cases respectively. In contrast, introduction of plausible $R_S$ values by the procedure indicated earlier resulted in finite limit damage projections for the terminally small node separation. The linear limits in those cases were 6.4% and 2.0 % for the Base Case-R and the Low DO$_2$ and $\rho$-R cases respectively.

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Figure 10 displays the same results in log-log format and provide additional insight on the overall trends. Ignoring the presence of $R_S$ results in trend lines with a nearly unity slope in the log-log graph over the entire range tested. When those trends were alternatively fit to a power law dependence of damage on active zone size exponents of 0.93 and 1.02 were obtained for the Base Case-NR and the Low $DO_2$ and $\rho$-NR cases respectively, confirming the nearly linear tendency toward a zero limit with decreasing zone size. In this display, the trends for the cases incorporating $R_S$ show as curves that, given the linear trend toward finite limits in Figure 9, tend toward horizontal asymptotes corresponding to those limits.

The damage prediction at 60 years for the equivalent of the Base Case-NR (diamond) but assuming $\beta_{CT} = \infty$ is shown in Figure, describing a system with a threshold invariant with potential. The dashed line represents a linear approximation showing a result, ~31% damage that is much greater than for the other cases and also essentially independent of the activation zone size. This independence is to be expected since in the absence of TDP each node in the column acts independently of the others so the result should be the same regardless of the choice of fineness of the segment sizes used. The result serves also as a positive check of the robustness of the calculation procedures. It is noted that the system is the same for which the $\beta_{CT} = \infty$ results are given in Figure 1. It is noted also that the relative damage level results for the various cases also met the expectation, noted earlier, that in Low $DO_2$ and $\rho$ conditions the damage should be less since the coupling effect between zones would be greater and the beneficial effect of TDP greater.

The results supports the validity of the hypothesis that as active zones become smaller their preventive throwing power would be reduced as well, resulting in the development of more numerous active zones that would make up for their individual smaller size in reaching to a finite damage terminal condition. Introducing the resistance polarization effect of $R_S$, resulted in a more realistic simulation of the extent to which a corroding zone prevents corrosion initiation in the surrounding regions. Conversely, the previous modeling approach projected unrealistically high prevention regions around existing corroding zones.

![Figure 9. Damage forecast for year 60 as function of activation zone size.](image-url)
CONCLUSIONS

- Exploratory calculations support the validity of the hypothesis that as active zones become smaller their preventive throwing power would be reduced as well, resulting in the development of more numerous active zones that would make up for their individual smaller size in reaching to a finite damage terminal condition.
- The model improvement over previous work stems from a more realistic implementation of the local concrete resistance $R_S$ around the reinforcing steel bars.
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